

# Possible nuclear fusion of deuteron in the cores of Earth, Jupiter, Saturn, and brown dwarfs

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## ABSTRACT

Many brown dwarfs have recently been discovered as sub-stellar objects in which deuteron thermonuclear fusion is taking place. Although Jupiter and Saturn emit nearly twice as much heat as they absorb from the Sun, their internal heat-generation mechanisms have been determined to differ from the nuclear fusion that fuels brown dwarfs because they have a mass factor of 0.023–0.077 less than that of brown dwarfs. The possibility for deuteron nuclear fusion in the Earth's core has not been well studied. Here, we compare the conditions for electron degeneracy pressure and temperature for the cores with an Fe–D compound of Earth, Jupiter, and Saturn to the core with deuterium gases of the coldest brown dwarf, WISE 1828+2650, in respect to three-body deuteron nuclear fusion, based on electron capture and internal conversion processes. Our results suggest that deuteron nuclear fusion is possible in the cores of Earth, Jupiter, and Saturn as well the coldest brown dwarf.

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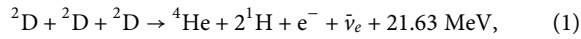
## I. INTRODUCTION

Brown dwarfs, bridging the gap between giant planets and hydrogen-fusing stars,<sup>1</sup> have recently been discovered as sub-stellar objects that do not have the mass required to sustain the nuclear fusion of ordinary hydrogen. However, they are understood to fuse deuterium as protostars.<sup>2</sup> Thus, they are also referred to as failed stars or super-Jupiters. Recently, temperate Earth-sized planets transiting a nearby ultra-cool brown dwarf (TRAPPIST-1, 2MASSJ23062928-0502285) were discovered.<sup>3</sup> In contrast, Jupiter is the largest planet in the solar system and is known as a failed brown dwarf because its mass  $M_J$  is less than 1.3%–7.7% of those of brown dwarfs.<sup>4</sup> Since sunlight, which drives the weather on Earth, is only 4% as strong on Jupiter as on Earth, Jupiter emits nearly twice as much heat as it absorbs from the Sun.<sup>5</sup> It is also known that Saturn and Neptune, as well as Jupiter, radiate about twice as much energy as they receive from the Sun.<sup>6</sup> When mass in a gravitationally bound object shrinks closer to the center of attraction, the gravitational potential energy converts into heat. It can be considered to be due to an exothermic reaction by adiabatic shrinkage.<sup>7</sup> This is known as the “Kelvin–Helmholtz mechanism” for the source of Jupiter's energy,<sup>8</sup> but it has been expanded by Bethe's theory of

nuclear fusion.<sup>9</sup> Other ideas, such as internal conversion of incident radiation into mechanical energy<sup>10</sup> and on-going tidal dissipation due to a non-zero planetary obliquity,<sup>11</sup> appear to lack general applicability.<sup>6</sup> The recent discovery of hot Jupiter exoplanets with insufficient eccentricity to be heated internally by tidal dissipation<sup>12</sup> has evoked much discussion as to possible sources of internal heat production.

Following the pioneering work of Kuroda<sup>13</sup> for natural fission reactors, much challenging work, such as planetocentric nuclear reactors by Herndon<sup>14</sup> and nuclear fission at the mantle boundary with the Earth's core by Meijer and van Westrenen,<sup>15</sup> has been carried out to explain thermal energy as the driving force of plate motion. The detection of antineutrinos in KamLand<sup>16</sup> and Borexino<sup>17</sup> was reported as evidence for natural fission. However, judging from a very small amount (12.5 ppm) of decaying product, Pb, in natural rocks and ores, the amount of decaying heat from radioactive materials would be not so large.<sup>18</sup> If radioactive decay has been occurring on other terrestrial planets, such as Mercury, Venus, Mars, and Earth's moon, which are Earth's sister planets with similar composition but smaller size, we would observe plate tectonics. Indeed, plate tectonics do not occur on these planets.<sup>18</sup> On the other hand, Fukuhara<sup>18,19</sup> proposed a model for the

origin of thermal energy within the Earth's interior, which is devoid of harmful radioactive waste, in which the generated heat is due to the three-body nuclear fusion of deuterium (D) confined within hexagonal FeDx core-center crystals,



where  $\bar{\nu}_e$  is an antineutrino. The deuteron-density-dependent fusion rate,  $R$ , and heat generation rate were calculated to be  $3.5 \times 10^{10}$  fusion/s/m<sup>3</sup> (supplementary material, Sec. 2) and  $1.27 \times 10^{15}$  J/m<sup>3</sup> (Ref. 19), respectively. The core volume, where fusion occurred, up through the present is  $4.99 \times 10^{17}$  m<sup>3</sup>. Because the relative pion exchange force is two and six for D–D and D–D–D simultaneous interactions,<sup>20</sup> we selected the 3D fusion in this study. Thus, the fusion rate of 3D is higher than that of 2D.

Recently, Jackson *et al.*<sup>21</sup> proposed a new model for the formation of the Earth's core, in which it was not extracted from the deep mantle, but derived from large impacts of other early solar system objects (containing FeO-rich silicates) with the proto-Earth. This model is consistent with our hypothesis on nuclear fusion, provided that they were enriched by D<sub>2</sub>O. The deuterium concentration in the center core with Fe–D compounds is a necessary condition for the fusion reaction.

In this study, we compare the relations of electron pressure and temperature for the cores with Fe–D compounds of Earth, Jupiter, and Saturn to the core with deuterium gases of the coldest brown dwarf, in respect of deuteron nuclear fusion. However, to the best of our knowledge, the possibility of deuteron nuclear fusion in the cores of Earth, Jupiter, and Saturn, as well as in the coldest brown dwarf, has not been studied.

## II. DEGENERATE ELECTRONS AND PION CONDENSATES IN THE CORES OF CELESTIAL BODIES

Various kinds of condensates are expected in the interior of the cores of celestial bodies, including degenerate electrons, neutrons in a superfluid state, protons in a superconducting state, and other exotic states, such as pion and kaon condensates.<sup>22,23</sup> We focus on degenerate electrons and meson condensates in brown dwarfs and the interior of planets with solid cores in the presence of a strongly interacting fermion system and their effects on the dynamics of deuteron thermonuclear fusion.

According to the free electron model by Zel'dovich and Novikov<sup>24</sup> and Al'tshuler and Bakanova,<sup>25</sup> the periodicity of metallic elements disappears under pressures greater than 100 GPa near the dwarf's inner core, which reflects the electronic shell structure of atoms. The outer and degenerate inner electrons behave like free electrons. Thus, we must use the Thomas–Fermi–Dirac model, which is usually thought of as being useful in predicting the properties of matter only at high densities and temperatures, taking into account the exchange energy.<sup>26</sup> In kinetic theory, the electron degeneracy gas pressure is given by the following equation:<sup>27</sup>

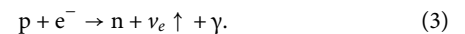
$$P = \frac{1}{5} \left( \frac{3}{8\pi} \right)^{\frac{2}{3}} \frac{h^2}{m} \left( \frac{N}{2} \right)^{\frac{5}{3}} \rho^{\frac{5}{3}}, \quad (2)$$

where  $m$ ,  $N$ , and  $h$  are the electron mass, Avogadro's number, and Planck's constant, respectively. The relationship is presented as a straight line at pressures above  $10^{15}$  Pa and densities about

$10^5 \text{ kg/m}^3$ . Jensen<sup>27</sup> calculated the isotherms for many metals at pressures below  $10^{15}$  Pa and densities below  $10^5 \text{ kg/m}^3$ . We calculate the degenerate electron gas pressures of Earth, Jupiter, and Saturn as there are insufficient pressure data available.

In contrast, the meson fields that mediate the interaction between nucleons can condense into a macroscopic state at high densities. This proceeds via a macroscopic excitation of the pion field when the density is high, and hence, the nucleons are interacting strongly, leading to a nonzero expectation value of the pion field in a broken symmetry state, such as the superconducting one. The charged and neutral pion condensed state would occur through a softening of a collective mode. In particular, the neutral condensed state is characterized by a spatially varying finite expectation value of the neutral pion field.<sup>28</sup> The surrounding clouds of pions produced by gluons have an influence on the strong, weak, and electromagnetic interactions under high pressure. The density of the cloud increases with the increase in the density of nucleons accompanied by the strong interaction although the density of the ordinary nucleus is almost constant regardless of elements.

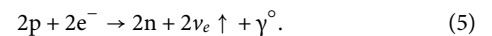
In degenerate electrons and meson condensates in the interiors of solid-core planets with Fe–D compounds and brown dwarfs with deuterons, the degenerate electrons suppress  $\beta^-$ -decay from neutron to proton and accelerate K-electron capture from the inner 1s state electrons within the nucleus. The electron capture process, based on the weak interaction, electromagnetically changes a proton to a neutron and simultaneously causes the emission of an electron neutrino  $\nu_e$ . Indeed, the radioactive decay constant measurement represents a pressure effect on the Be<sup>7</sup> capture rate.<sup>29</sup> Because the deuterium daughter nuclide under high pressure is in an excited state, it emits a gamma ray,  $\gamma$ , by transition from excited to ground states. Since the deuterons in solids are trapped by periodic potential, the pairing partner of deuteron limits to the neighboring deuteron. In this case, a high-energy electron resulting from internal conversion induces the emission of high-speed gamma rays, which may be massive bosons, from the s shell orbit surrounding the deuterium nucleus into the nuclei of the neighboring deuterons. The electron capture and internal conversion processes are simultaneously described as



The neutral pion in Eq. (3) is provided by the high-energy gamma rays via the fundamental process of electromagnetic interactions,<sup>30</sup>

$$\gamma + \gamma = \pi^0. \quad (4)$$

From Eqs. (3) and (4), the electrons and protons in two deuterons react with each other to form two neutrons, two electron neutrinos, and one neutral pion,



The electron and neutral pion velocities are calculated to be  $2.73 \times 10^7$  m/s and  $1.68 \times 10^6$  m/s, respectively (supplementary material, Sec. 1). The lifetime of the resulting neutral pion is  $2.38 \times 10^{-17}$  s ( $= 4.01 \times 10^{-11}$  m/ $1.68 \times 10^6$  m/s), which is slightly less than the lifetime [ $9.5 \pm 1.5 \times 10^{-17}$  s (Ref. 31)] of the neutral pion, provided that the neutral pion is formed in the space [ $4.01 \times 10^{-11}$  m (Ref. 18)] between the two neighboring shrunken deuterons. Indeed, because the Oppenheimer–Phillips paper indicates that the range of the nucleonic portion of the deuteronic wave-function extends to

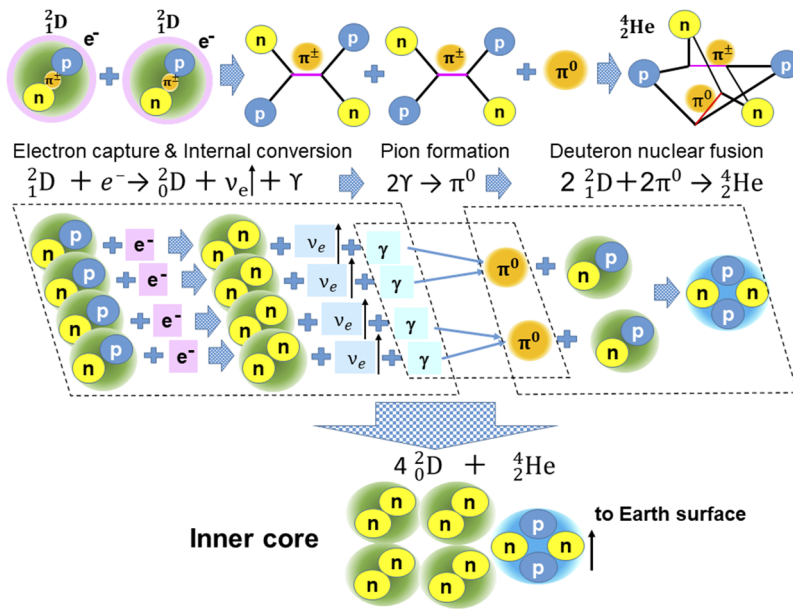


FIG. 1. Schematic presentation of deuteron nuclear fusion based on electron capture and internal conversion processes.

about 5 F (Ref. 32), the lifetime would be less than  $2.97 \times 10^{-21}$  s ( $= 5 \times 10^{-15}$  m/ $1.68 \times 10^6$  m/s). This value is considerably smaller than the lifetime of a neutral pion. Therefore, the formation of the He nucleus from the fusion of two deuterons requires a direct force caused by the exchange of two neutral pions that do not compose the deuteron nucleus because the additional non-exchange part mediated by the neutral pion substantially moderates the  $n$ - $p$  force in the He nucleus,<sup>33</sup>

$${}^2_1\text{D} + {}^2_1\text{D} + 2\pi^0 = {}^4_2\text{He}. \quad (6)$$

As a result, we can deduce mix products of  ${}^4_2\text{D}$  and  ${}^4_2\text{He}$  in the center of the core. The neutrinos are released from the Earth's interior to the Universe. These processes are illustrated schematically in Fig. 1.

### III. NUCLEAR FUSION IN THE CORES OF CELESTIAL BODIES

#### A. Earth

For the compressed core of Earth, we calculated the electron degeneracy gas pressure,  $P$ , at a high temperature of 5130–6370 K and a high density of  $13\,780$ – $13\,970$  kg/m<sup>3</sup> of  $\epsilon$ -Fe at  $377 \pm 8.5$  GPa in the Earth's core.<sup>34</sup> From Jensen's calculated isotherm diagrams,<sup>27</sup> we obtain a pressure of 1.0–1.2 TPa. For deuteron thermonuclear fusion reactions that require occurring in celestial bodies, the following conditions at their centers are necessary: a large amount of deuterium and a high-temperature and high-pressure environment to overcome the high Coulomb barrier for fusion reactions. However, the definition for deuteron nuclear fusion needs to be extended from gaseous deuterium objects, such as brown dwarfs, to planets with solid cores containing deuterons, such as Earth, Jupiter, and Saturn.

We next compare the electron pressure effect for the cores of Earth and a brown dwarf. In sharp contrast to the brown dwarf with an inner core of deuterium gas, Earth is a rocky planet with a core

of an Fe-based compound. The deuterium atoms of the former are packed by quantum electron degeneracy pressure alone, whereas the deuterium atoms of the latter are served by the squeezing effect of 26 electrons surrounding the Fe nucleus in the tetrahedral sites of the  $\epsilon$ -Fe lattice.<sup>34</sup> Figure 2 shows comparative schematics of a D atom squeezed by a tetrahedral Fe atom lattice in the core of Earth and a squeezed D atom in a brown dwarf's core. We obtain a multiplied confinement effect of 0.229 ( $= 0.517 \times 0.443$ ) (supplementary material, Sec. 4) for the D–D distance. Thus, the confinement effect of the latter is more effective than that of the former.

We then consider a physical catalysis effect for the dynamic reactions of deuteron pairs, based on the formation of neutral pions.

#### D atom squeezed by tetrahedral Fe atom lattice in Earth's core

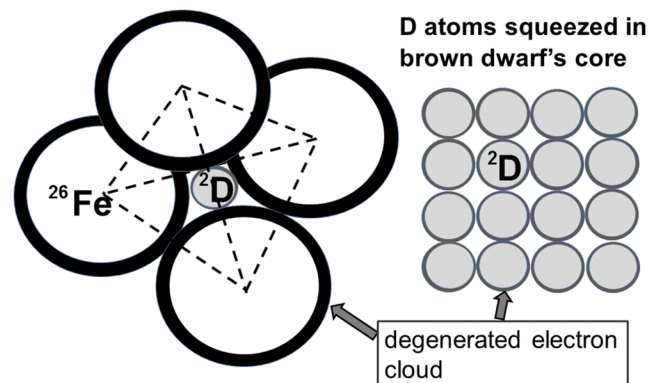


FIG. 2. Schematic of the two squeezing effects by 26 electrons surrounding the Fe in the tetrahedral sites of  $\epsilon$ -Fe lattices in the Earth's core and quantum electron degeneracy pressure in a brown dwarf's core.

The effect can be described by the enhancement of the attractive interaction force by a factor of 14 ( $= 2 \times 7$ ) via two neutral pions. Kenny<sup>35</sup> reported that the attraction caused by the exchange of one neutral pion with the spin zero boson is seven times larger than the nucleonic constituents, such as protons and neutrons. He named the mass formula “electropionics.” Deuteron fusion results from the reduction in the D–D distance to 0.0284 nm by the multiplied effect of physical catalysis (supplementary material, Sec. 4). Although there is possibility that some momentum transfers to one of the deuterons to cause barrier penetration, we neglect the problem in this study.

## B. Jupiter

It is estimated that Jupiter has a central core of solid matter, which is composed of mostly iron and silicate minerals (similar to quartz) and could have a temperature of 50 000 K (Ref. 36), which is hotter than the surface of the Sun. The total mass of heavy elements (core + molecular envelope) is between 11 and 45 times that of the Earth’s core and 4–14% the total mass of Jupiter.<sup>37</sup> As the core density of Jupiter is estimated to be  $2.5 \times 10^4 \text{ kg/m}^3$  (Ref. 38), we can calculate the electron degeneracy gas pressure as  $5.2 \pm 0.5 \text{ TPa}$  from Jensen’s isotherm diagram.<sup>27</sup> The amount of deuterium in the core of Jupiter can be derived from the late veneer’s bombardment of comets and meteorites with  $\text{H}_2\text{O}$  and  $\text{D}_2\text{O}$  originating from the Kuiper belt or planetesimals between Mars and Saturn, as well as in the primitive dry Earth.<sup>39,40</sup>

## C. Saturn

Since Saturn, the second largest planet of the solar system, also radiates 2–3 times [ $2 \times 10^{17} \text{ W}$  (Ref. 41)] as much heat as it receives from the Sun, it must have an internal heat source; however, there is not enough evidence to explain the heat production. Saturn’s core is made mostly of rocky and metal elements similar to Jupiter’s core.<sup>42</sup> The core’s temperature is around 22 000 K (Ref. 43). The mass of the core is larger than Jupiter’s core. (For comparison, Jupiter is 317.8 Earth masses and Saturn is 95.2 Earth masses.)<sup>44</sup> Since the core density of Saturn is estimated to be  $2.05 \times 10^4 \text{ kg/m}^3$  (Ref. 45), we can calculate the electron degeneracy gas pressure as  $3.0 \pm 0.5 \text{ TPa}$  from Jensen’s isotherm diagram.<sup>27</sup> The amount of deuterium in the core of Saturn could be delivered from comets and meteorites with  $\text{H}_2\text{O}$  and  $\text{D}_2\text{O}$ , as well as in the primitive Jupiter and Earth.<sup>39,40</sup>

Since we cannot get precise temperature, pressure, and density measurements of Neptune’s core, we could not calculate the pressure–temperature condition.

## D. Brown dwarfs

Brown dwarf interior models provide the following density ( $\rho_c$ ) condition:<sup>2</sup>

$$10 \text{ g/cm}^3 \leq \rho_c \leq 1000 \text{ g/cm}^3. \quad (7)$$

Recently, Beichman *et al.*<sup>46</sup> discovered the coldest Y brown dwarf, WISEPAJ182831.08 + 265 037.8, with a surface temperature of 300 K. The degeneracy electron gas pressure can be calculated as  $370 \text{ GPa} < P < 31.2 \text{ PPa}$  for  $1 \times 10^4 \text{ kg/m}^3 < \rho_c < 1 \times 10^6 \text{ kg/m}^3$  from Jensen’s isotherm diagram<sup>27</sup> and Eq. (7) at pressure below and above  $10^{15} \text{ Pa}$ , respectively.

In contrast, as the mass of the brown dwarf is  $0.0029\text{--}0.0057 M_\odot$  (solar mass),<sup>46</sup> the peak ( $T_c$ ) of the mass-dependent core temperature for the brown dwarf can be calculated by the following equation:<sup>47</sup>

$$T_c \sim 2 \times 10^6 \text{ K} \left( \frac{M}{0.05 M_\odot} \right)^{4/3}. \quad (8)$$

The core temperatures of dwarfs increase with age, reach a peak, and then decrease. From Eq. (8), we obtain a  $T_c$  of  $4.49 \times 10^4\text{--}1.11 \times 10^5 \text{ K}$  for the brown dwarf’s mass of  $0.0029\text{--}0.0057 M_\odot$ .

## IV. PRESSURE–TEMPERATURE RELATIONS FOR DEUTERIUM NUCLEAR FUSION

Here, we note the Lawson criterion, which defines the conditions required for hydrogen nuclear fusion reactors.<sup>48</sup> The “triple product” of plasma (electron) density  $n_e$ , confinement time  $\tau$ , and plasma temperature  $T$  is valid for nuclear ignition of homogeneous hydrogen plasma,

$$n_e \tau > \frac{12 k_B T}{\langle \sigma v \rangle Q}, \quad (9)$$

where  $\sigma$  and  $Q$  are the cross section and the binding energy of fusion products, respectively, and  $\langle \rangle$  denotes an average over the Maxwellian velocity distribution. According to the Maxwellian molecular speed distribution for gases, the speed distribution of plasma gases with higher density and temperature draws near to Gaussian distribution. Since the confinement time for natural nuclear fusion in the cores of celestial bodies is infinite, we use the modified criterion using the electronic pressure (electron density) and temperature. Thus, it is necessary for the validation of fusion to analyze natural instances of electron degeneracy pressure–temperature conditions. Figure 3 presents the relation of electron pressure and temperature for three instances: possible nuclear fusion in the cores of Earth at 5130–6370 K under 1.0–1.2 TPa, Jupiter at 50 000 K under  $5.2 \pm 0.5 \text{ TPa}$ , and Saturn at 22 000 K under  $3.0 \pm 0.5 \text{ TPa}$ ; nuclear fusion in the core of the coldest brown dwarf at  $4.49 \times 10^4\text{--}1.11 \times 10^5 \text{ K}$  under 0.37–31.2 TPa; and hydrogen thermonuclear fusion in the Sun’s core at  $1.57 \times 10^7 \text{ K}$  (Ref. 49) under

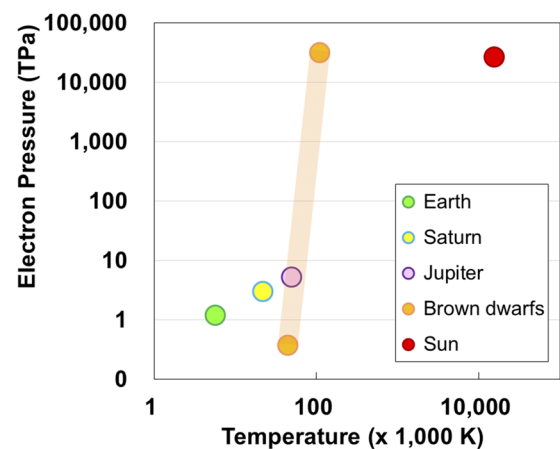


FIG. 3. Electron pressure–temperature conditions in the cores of Earth, Jupiter, Saturn, brown dwarfs, and the Sun.



$2.65 \times 10^{11}$  bar (26.5 PPa).<sup>50</sup> The uncertainty of the data is smaller than the symbol size used in Fig. 3. The pressure–temperature conditions of Earth, Jupiter, and Saturn are near the criterion of the coldest brown dwarf. Jupiter, in particular, could be a brown dwarf, in which deuteron thermonuclear fusion is taking place. It is known that the condition of low temperature and high density lies in low temperature nuclear fusion, such as deuteron fusion in contrast to hydrogen nuclear fusion of high temperature and low density.<sup>51</sup>

Finally, we compare the “double product,”  $\zeta$ , of the pressure (electron density) and temperature for the cores of Earth, Jupiter, and Saturn to those of the coldest brown dwarf with  $4.49 \times 10^4$  K and 370 GPa. The cores of Earth, Jupiter, and Saturn show  $\zeta = 0.31$  [(5130 K/44 900 K)  $\times$  (1.0 TPa/0.37 TPa)]–0.46 [(6370 K/44 900 K)  $\times$  (1.2 TPa/0.37 TPa)], 15.65 [(50 000 K/44 900 K)  $\times$  (5.2 TPa/0.37 TPa)], and 3.97 [(22 000 K/44 900 K)  $\times$  (3.0 TPa/0.37 TPa)], respectively. Since large  $\zeta$  plays a decisive role in the deuteron nuclear fusion, Saturn would also be a member of the group of brown dwarfs. Furthermore, there is a possibility that the deuteron nuclear reaction occurs discontinuously in the Earth’s core, taking the multiplied effect of D atoms squeezed by tetrahedral Fe atom lattices in the core of Earth into consideration. The details are described in the [supplementary material](#), Sec. 4.

The proposed 3D fusion process requires a solid inner core with Fe–D crystals. The cores of Earth, Jupiter, and Saturn provide a necessary and sufficient condition (temperature over 50 000 K and electron pressure over 0.37 TPa) for deuteron thermonuclear fusion. However, it needs further investigation for 2D and 3D reactions in the cores of celestial bodies because it is not an untestable hypothesis.

## V. GEOLOGICAL IMPLICATIONS OF DEUTERON FUSION IN THE INNER CORE OF EARTH

When fusion takes place in a random phase, such as gas or plasma in brown dwarfs, the macroscopic fusion rate is proportional to the square of the deuteron density. However, the microscopic fusion rate in solids is proportional to the deuteron density, because of the drastic decrease of freedom in deuterons in solids.<sup>52</sup> Even if deuteron–nuclear fusion in the cores of Earth, Jupiter, and Saturn does occur, the nuclear reaction does not follow a chain reaction because of the heterogeneous distribution of deuterons squeezed in solid iron and suppression controlled by the deuteron concentration. A collective resonance by three-dimensional electron charge density wave based on the breathing-mode displacement (see the [supplementary material](#), Sec. 4 of Ref. 18) does not occur continuously. Thus, the heat generated by the deuteron thermonuclear fusion would not so much as melt the inner core.

The fusion heat generated after the formation of the inner core transfers to the outer liquid core. A vast sea of electrically conducting molten iron fluid circulates at the outer core, constituting the so-called geodynamo. Evidence from the geologic record shows that the orientation of the dynamo has flipped from north to south and back again hundreds of times during Earth’s 4.5-billion-year history. The polarity reversals are explained by the proliferation, growth, and poleward migration of reversed flux patches, which originate at only four broad regions on the core–mantle boundary.<sup>53</sup> Thus, there is a possibility that discontinuous fusion events have an influence on the destruction of the original

polarity and generation of the new polarity. Our hypothesis will explain why plate tectonics exist on Earth but not on other terrestrial planets, such as Mercury, Venus, Mars, and moon, provided that the antineutrinos from Jupiter, Saturn, and brown dwarfs are detected.

## VI. CONCLUSIONS

We provide a possible model for the origin of thermal energy from interiors of Earth, Saturn, and Jupiter without radioactive wastes, in which heat generation is the result of three-body fusion of deuterons confined within hexagonal FeD core–center crystals. From the viewpoint of deuteron nuclear fusion, we compared the relations of electron degenerate pressure and temperature for the cores of Earth, Jupiter, and Saturn to that of the coldest brown dwarf, using data of published articles. The thermal nuclear fusion would be occurring in the cores of Earth, Saturn, and Jupiter, as well as those of brown dwarfs.

## SUPPLEMENTARY MATERIAL

See the [supplementary material](#) for degenerate electrons and pion condensates in the Earth’s core, the nuclear reaction rate of the deuteron thermonuclear fusion, possible occurrence of excited electrons and neutral pion catalysis, and calculation of the critical temperature and pressure under confinement by high-temperature and physical catalysis effects.

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## DATA AVAILABILITY

The data that support the findings of this study are available within the article (and its [supplementary material](#)).

## REFERENCES

- <sup>1</sup>S. R. Kulkarni, *Science* **276**, 1350 (1997).
- <sup>2</sup>F. Allard and D. Homeier, *Scholarpedia* **2**, 4475 (2007).
- <sup>3</sup>M. Gillon, E. Jehin, S. M. Lederer, L. Delrez, J. de Wit, A. Burdanov, V. Van Grootel, A. J. Burgasser, A. H. M. J. Triaud, C. Opitom, B.-O. Demory, D. K. Sahu, D. B. Gagliuffi, P. Magain, and D. Queloz, *Nature* **533**, 221 (2016).
- <sup>4</sup>A. Burrows, W. B. Hubbard, D. Saumon, and J. I. Lunine, *Astrophys. J.* **406**, 158 (1993).
- <sup>5</sup>A. Seiff, *Nature* **403**, 603 (2000).
- <sup>6</sup>J. M. Herndon, *Curr. Sci.* **96**, 1453 (2009).
- <sup>7</sup>T. Guillot, D. J. Stevenson, W. B. Hubbard, D. Saumon, F. Bagenal, T. E. Dowling, and W. B. McKinnon, “The interior of Jupiter,” in *Jupiter: The Planet, Satellites and Magnetosphere* (Cambridge University Press, New York, 2004), Chap. 3.
- <sup>8</sup>B. W. Carroll and D. A. Ostlie, *An Introduction to Modern Astrophysics*, 2nd ed. (Cambridge University Press, New York, 2007), pp. 296–298.
- <sup>9</sup>J. P. Horgan and A. B. Hans, *Sci. Am.* **267**, 32 (1992).
- <sup>10</sup>A. P. Showman and T. Guillot, *Astron. Astrophys.* **385**, 166 (2002).
- <sup>11</sup>J. N. Winn and M. J. Holman, *Astrophys. J.* **625**, L159 (2005).
- <sup>12</sup>P. Bodenheimer, D. N. C. Lin, and R. A. Mardling, *Astrophys. J.* **548**, 466 (2001).
- <sup>13</sup>P. K. Kuroda, *J. Chem. Phys.* **25**, 1295 (1956).

- <sup>14</sup>J. M. Herndon, *Naturwissenschaften* **79**, 7 (1992).
- <sup>15</sup>R. J. de Meijer and W. van Westrenen, *S. Afr. J. Sci.* **104**, 111 (2008).
- <sup>16</sup>T. Araki *et al.*, *Nature* **436**, 499 (2005).
- <sup>17</sup>G. Bellini *et al.*, *Phys. Lett. B* **687**, 299 (2010).
- <sup>18</sup>M. Fukuhara, *Sci. Rep.* **6**, 37740 (2016).
- <sup>19</sup>M. Fukuhara, *Sci. Rep.* **7**, 46436 (2017).
- <sup>20</sup>A. Takahashi, T. Iida, T. Takeuchi, and A. Mega, *Int. J. Appl. Electromag. Mag.* **3**, 221 (1992).
- <sup>21</sup>C. R. M. Jackson, N. R. Bennet, Z. Du, E. Cottrell, and Y. Fei, *Nature* **553**, 491 (2018).
- <sup>22</sup>G. Baym and C. Pethick, *Annu. Rev. Nucl. Part. Sci.* **25**, 27 (1975).
- <sup>23</sup>V. Dwivedi, "Condensates in neutron star interiors," Emergent States of matter: Fall 2011 Term Essays, the University of Illinois at Urbana-Campaign, pp. 1–11, [https://pdfs.semanticscholar.org/9411/33d026d99dae4a8ba8142e6b401c7e6f5bc.pdf#search=%27Vatsal+Dwivedi%2C+Condensates+in+N](https://pdfs.semanticscholar.org/9411/33d026d99dae4a8ba8142e6b401c7e6f5bc.pdf#search=%27Vatsal+Dwivedi%2C+Condensates+in+Neutron+Star+Interiors%27)
- <sup>24</sup>Ya. B. Zel'dovich and I. D. Novikov, *Relativistic Astrophysics* (Chicago University Press, Chicago, 1971), Vol. 1, p. 161.
- <sup>25</sup>L. V. Al'tshuler and A. A. Bakanova, *Soviet. Phys. Uspekhi* **11**, 678 (1969).
- <sup>26</sup>M. Ross and B. J. Adler, *J. Chem. Phys.* **47**, 4129 (1967).
- <sup>27</sup>S. D. Hamann, *Physico-Chemical Effects of Pressure* (Butterworths Scientific Publications, San Francisco, 1957), p. 58.
- <sup>28</sup>G. Baym, *Nucl. Phys. A* **690**, 233 (1995).
- <sup>29</sup>L. Liu and C. Huh, *Earth Planet. Sci. Lett.* **180**, 163 (2017).
- <sup>30</sup>L. Aphenetche *et al.*, *Phys. Lett. B* **519**, 8 (2001).
- <sup>31</sup>H. A. Atherton, C. Bovet, P. Coet, R. Desalvo, N. Doble, R. Maleyran, E. W. Anderson, G. Von Dardel, K. Kulka, M. Boratav, J. W. Cronin, and B. D. Milliken, *Phys. Lett. B* **158**, 81 (1985).
- <sup>32</sup>J. T. Waber and M. de Llano, *Trans. Fusion Technol.* **26**, 496 (1994).
- <sup>33</sup>M. Fukuhara, *Fusion Sci. Technol.* **43**, 128 (2003).
- <sup>34</sup>S. Tatenno, K. Hirose, Y. Ohishi, and Y. Tatsumi, *Science* **330**, 359 (2010).
- <sup>35</sup>J. Kenny, *Fusion Technol.* **19**, 547 (1991).
- <sup>36</sup>P. Davis, "Jupiter: In depth," in Planets-NASA Solar System Exploration, NASA Planetary Science Division, NASA's Jet Propulsion Laboratory, 2016, <https://solarsystem.nasa.gov/planets/jupiter/indepth>.
- <sup>37</sup>T. Guillot, D. Gautier, and W. B. Hubbard, *Icarus* **130**, 534 (1979).
- <sup>38</sup>J. Papiewski, "Jupiter's core vs. Earth's core," Sciencing, Astronomy, 2017, <http://sciencing.com/jupiter-core-vs-earths-core-21848.html>.
- <sup>39</sup>F. Robert, *Science* **293**, 1055 (2001).
- <sup>40</sup>R. Meier, T. C. Owen, H. E. Matthews, D. C. Jewitt, D. Bockelée-Morvan, N. Biver, J. Crovisier, and D. Gautier, *Science* **279**, 842 (1998).
- <sup>41</sup>M. Porter, "Saturn spectacular rings and mysterious Moons," in *The Jovian Planets, Part II, Saturn* (SlidePlayer, Inc., 2015), Chap. 12, <http://slideplayer.com/slides/6039759/>.
- <sup>42</sup>P. Davis, "Saturn: In depth," in Planets-NASA Solar System Exploration, NASA Planetary Science Division, NASA's Jet Propulsion Laboratory, 2009, <https://solarsystem.nasa.gov/planets/saturn/indepth>.
- <sup>43</sup>S. Lipoff, "What is Saturn's core made of?" Sciencing, Astronomy, 2017, <https://sciencing.com/saturns-core-made-5068007.html>.
- <sup>44</sup>J. J. Fortney, *Science* **305**, 1414 (2004).
- <sup>45</sup>N. Miller, J. J. Fortney, and B. Jackson, *Astrophys. J.* **702**, 1413 (2009).
- <sup>46</sup>C. Beichman, R. G. Christopher, J. D. Kirkpatrick, T. S. Barman, K. A. Marsh, M. C. Cushing, and E. L. Wright, *Astrophys. J.* **764**, 1 (2013).
- <sup>47</sup>N. Lodieu, *A Theoretical and Observational Overview of Brown Dwarfs* (Instituto de Astrofísica de Canarias, La Laguna, Tenerife, Spain, 2017), p. 14, [www.iac.es/galeria/nlodieu/media/articles/chapter1](http://www.iac.es/galeria/nlodieu/media/articles/chapter1).
- <sup>48</sup>R. G. Mills, *IEEE Trans. Nucl. Sci.* **18**, 205 (1971).
- <sup>49</sup>J. N. Bahcall and M. H. Pinsonneault, *Rev. Mod. Phys.* **67**, 781 (1995).
- <sup>50</sup>D. H. Hathaway, "The solar interior," Solar Physics, Marshall Space Flight Center, NASA, 1–3, 2015, <https://solarscience.msfc.nasa.gov/interior.shtml>.
- <sup>51</sup>N. Wada, *Trans. Mater. Res. Soc. Jpn.* **2**, 102 (1992).
- <sup>52</sup>A. Takahashi, T. Iida, H. Miyamaru, and M. Hukuhara, *Fusion Technol.* **27**, 71 (1995).
- <sup>53</sup>G. A. Glatzmaier and P. Olsen, *Sci. Am.* **292**, 50 (2005).

## Supplementary material

# Possible nuclear fusion of deuteron in the cores of Earth, Jupiter, Saturn and brown dwarfs

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## 1. Degenerate electrons and pion condensates in Earth's cores

We first explain an electron capture in  ${}^2\text{H}$  using FIG 1. Since electron-capture decay rates depend on the density of atomic electrons within the nucleus, external factors such as chemical form and pressure alter the electron overlap densities with the nucleus and thus affect the electron-capture decay rates. Since one electron of 1s in  ${}^2\text{H}$  is degenerated under high pressure of  $377 \pm 8.5$  GPa, a proton in  ${}^2\text{H}$  captures easily the 1s electron to form a neutron and simultaneously emits an electron neutrino.



Since the 26 electrons of Fe atom surrounding the squeezed  ${}^2\text{H}$  atom in Fe-0.6wt% D crystal near inner core are also degenerated, one electron of Fe atom transports momentarily to an electron hole. The total electron weight of Fe in Fe-0.6 wt% D is calculated as

$$26 \times 9.1094 \times 10^{-31} \text{ (kg)} \times 7.44 / (7.44 + 0.3) = 2.28 \times 10^{-29} \text{ kg}, \quad (\text{S2})$$

where the volume of  $\epsilon$ -Fe and D in Fe-0.6 wt% D can be estimated as 7.44 cm<sup>3</sup> and 0.3 cm<sup>3</sup>, respectively.<sup>18</sup> The volume ratio, calculated using weight ratio, is  $4.09 \times 10^{-28}$  ( $2.28 \times 10^{-29}$  kg/55.65 kg). Since total volume of Fe-D crystal is  $6.23 \times 10^{16}$  m<sup>3</sup>, the electron volume belonging to Fe is

$$6.23 \times 10^{16} \text{ (m}^3\text{)} \times 4.09 \times 10^{-28} = 2.55 \times 10^{-11} \text{ m}^3. \quad (\text{S3})$$

Thus we can obtain total electron charge belonging to Fe using electron pressure of 1.2 TPa.

$$1.91 \times 10^{20} \text{ eV} (= 1.2 \times 10^{12} \text{ (Pa)} \times 2.55 \times 10^{-11} \text{ (m}^3\text{)} / (1.602 \times 10^{-19} \text{ (J)})) \quad (\text{S4})$$

The excited electron  $e^*$  from Fe which falls to 1s electron hole of D under high pressure emits simultaneously a gamma ray  $\gamma$ .

$$e^* \rightarrow e^- + \gamma \quad (\text{S5})$$

The velocity of a high-energy electron is given by

$$\frac{1}{2} m_e V_e^2 = 1.91 \times 10^{14} \text{ (MeV)} \quad (\text{S6})$$

$$m_e = 0.511 \text{ MeV} \quad (\text{S7})$$

$$V_e = 2.73 \times 10^7 \text{ m/s}, \quad (\text{S8})$$

where  $m_e$  is the masses of the electron. If two gamma rays convert to a neutral pion in neighbour shrunken deuterium atom ( $d = 4.01 \times 10^{-11}$  m),<sup>18</sup> we can calculate a velocity of a neutral pion. Indeed, the range of the conversion would be within deuteronic wave-function of about 5 fm.<sup>32</sup>

$$\gamma + \gamma = \pi^0. \quad (\text{S9})$$

From Eq. (S9), we find that

$$\frac{1}{2} m_{\pi^0} V_{\pi^0}^2 = \left[ \frac{1}{2} m_{\pi^0} V_{\pi^0}^2 \right]_{D-Dd} \quad \text{and} \quad m_{\pi^0} = \left[ m_{\pi^0} \right]_{D-Dd}$$



$$V_{\pi^0} = \sqrt{\frac{2m_n}{m_n + m_{\pi^0}}} \sqrt{E_{D-Dd} - 2m_n c^2}$$

where  $m_{\pi^0}$  is the masses of the neutral pion.

## 2. Nuclear reaction rate of the deuteron thermonuclear fusion

From Eq. (S1), we calculate velocity  $V_n$  of the neutron, using neutron mass  $m_n$ .

$$\frac{1}{2} m_n V_n^2 = \frac{1}{2} \left( \frac{m_n}{m_n + m_{\pi^0}} \right) \sqrt{E_{D-Dd} - 2m_n c^2}$$

$$m_n = 939.55 \text{ MeV} \quad (\text{S14})$$

$$V_n = 6.37 \times 10^5 \text{ m/s.} \quad (\text{S15})$$

We then calculate velocity  $V_D$  of D for reaction  $D \rightarrow n + H$ .

$$\frac{1}{2} m_n V_n^2 = \frac{1}{2} M_D V_D^2 \times$$

(S16)

$$m_D = m_p + m_n \quad (\text{S17})$$

We obtain  $V_D = 4.51 \times 10^5 \text{ m/s}$ .

When one neutral pion collides with one deuteron in Eq. (6), we find that

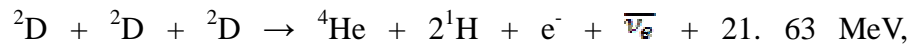
$$2 \times \frac{1}{2} m_{\pi^0} V_{\pi^0}^2 = \frac{1}{2} M' V_{M'}^2, \quad (\text{S18})$$

$$M' = m_p + m_n + m_{\pi^+} + m_{\pi^0}, \quad (\text{S19})$$

where  $m_p$  and  $m_{\pi^+}$  are the masses of the proton (= 938.27 MeV) and charged pion (139.6 MeV), respectively, activated state product of  $M'$ , and  $V_{M'}$  is velocity of  $M'$ , provided that the mass deviation energy is negligible.  $V_{M'}$  is calculated as

$$V_{M'} = 5.96 \times 10^5 \text{ m/s.} \quad (\text{S20})$$

The 3D thermonuclear fusion was described at Supplementary Information 8 of previous paper.<sup>18</sup>



(S21)

The third D further collides with  $M'$  in Eq. (S19), yielding He and 2H.

$$\frac{1}{2} \times M_D V_D^2 = \frac{1}{2} \times M'' [V_{\downarrow}(M'')]^2 \quad (S22)$$

$$M'' = m_p + m_n + m_{\pi^{\pm}} + m_{\pi^0} + 2 m_p, \quad (S23)$$

where  $M''$  is the activated state DDD of Eq. (S21). Hence, the velocity of the reduced mass of DDD is

$$V_{M''} = 3.08 \times 10^5 \text{ m/s} \quad (S24)$$

To obtain the Coulomb factor,  $H_0^2$ , we must calculate  $\eta$ .

$$H_0^2 \cong 2\pi\eta \exp(-2\pi\eta) \quad (S25)$$

$$\eta = \frac{e^2}{\hbar V_{M''}} \quad (S26)$$

where  $\eta$  is the Sommerfeld parameter.

From Eq. (S26), we obtain

$$\eta = \frac{e^2}{\hbar V_{M''}} = \frac{1.44}{V_{M''} \text{ (in MeV)}}$$

Substituting Eq. (S27) for Eq. (25), we obtain

$$\begin{aligned} H_0^2 &= 2\pi \times 7.11 \exp(-2\pi \times 7.11) \\ &= 1.74 \times 10^{-18}. \end{aligned} \quad (S28)$$

Eqs. (S27) and (S28) lead to the familiar Gamow formula<sup>54</sup>

$$\sigma = \frac{S}{E} \frac{1}{2\pi\eta_0} \exp(-2\pi\eta_0) = \frac{S}{E} \exp\left(-\frac{\beta}{\sqrt{E}}\right) \quad (S29)$$

Thus we can obtain a production cross section  $\sigma$  in Eq. (S30), using  $B = 2 \times 10^{-8} \text{ cm}^3/\text{s}$  (Ref. 55), based on the catalytic help of neutral pions.

$$\sigma = \frac{2.0 \times 10^{-8} \times 1.7 \times 10^{-18}}{3.08 \times 10^7} = 1.13 \times 10^{-26} \text{ cm}^2 = 1.13 \times 10^{-2} \text{ barn} \quad (\text{S30})$$

The reduced energy of masses  $m_1$  and  $m_2$  of incident particle and a target nucleus, using the astrophysical  $S$  factor ( $=10^{11}$  keV barn) by four orders of magnitude with respect to the conventional condition of two charged pions. Eq. (S31) gives

$$E = \frac{E_{m_2}}{E_{m_1} + E_{m_2}} \quad (\text{S31})$$

$$= \frac{10^{11} \text{ (keV barn)}}{1.03 \times 10^{-2} \text{ (barn)}} \times 1.74 \times 10^{-18} = 0.0154 \text{ eV} \quad (\text{S32})$$

This value is plausible for neutral pion catalyzed nuclear fusion within a D-D-D system. Substituting  $\sigma = 1.13 \times 10^{-2}$  barn,  $S = 10^{11}$  keV barn for the D-D-D reaction and  $E = 0.015$  eV into Eq. (S29) gives the Coulomb barrier tunnelling constant

$$\beta = 5.07 \text{ eV}. \quad (\text{S33})$$

Thus, we have the Gamow formula

$$\sigma = \frac{10^{11}}{E} \exp\left(\frac{-5.1}{\sqrt{E}}\right) \quad ((\text{[ ]})^{\wedge})/((\text{[ ]})^{\wedge}))/((\text{[ ]})^{\wedge})_{\text{D-}}$$

The nuclear reaction rate/cm<sup>3</sup> is given by

$$R = N_D N_{coh} V_M \sigma \quad (\text{S35})$$

where  $N_D$  is the deuteron number of density, and  $N_{coh}$  is the multiplicity factor according to lattice-site conditions. Because  $N_D$  increases as the inverse of the cubic function of the radius ratio  $(2r_3/2r_1)^3 = (0.02075/0.074)^3 = 1/45.4$ , we use  $N_D = 10^{22}/\text{cm}^3$ . If  $N_{coh} = 10/\text{cm}^3$  (Ref. 56), we obtain

$$R = 10^{22} (1/\text{cm}^3) \times 10 (1/\text{cm}^3) \times 3.08 \times 10^7 (\text{cm/s}) \times 1.13 \times 10^{-26} (\text{cm}^2) = 3.48 \times 10^4 \text{ fusion/s/cm}^3$$

$$\cong 3.5 \times 10^{10} \text{ fusion/s/m}^3 \quad (\text{S36})$$

### 3. Possible occurrence of excited electrons and neutral pion catalysis

In main text, with a view to promoting facilitating the electropionic attraction, the excited electron capture and the neutral pion catalysis were investigated. Here we consider a possibility for formation of the excited electrons and neutral pion catalysis from view of geoscience.

The seismic electromagnetic activities, radio wave emission, lightening, *etc.*, are explained by the electrical response of rocks with and without quarts.<sup>57,58</sup> Especially, exoelectron emission signals are associated with stick-slip of solids along heat flow under high pressure,<sup>59</sup> and by cyclic expansion and contraction due to lunar gravitation, as well as “pressure ionization”<sup>60</sup> generated under pressures greater than 100 GPa within dense astrophysical objects (substellar objects, white dwarfs, giant planets *etc.*). These natural events would become a source of excited electrons.

Tsutsumi and Shirai<sup>61</sup> observed effect of stress on the intensity of the electric signal in stick-slip experiments on quartz-free rock specimens of basalts at confining process of up to 120 MPa. The relation between amplitude of electric field change ( $V_f$ ) and shear stress drop ( $P_d$ ) is presented at Fig. 1S. We get the following relation.

$$V_f = 0.0025P_d^2 + 0.0901 P_d + 1.5007 \quad (R^2 = 0.9993). \quad (\text{S37})$$

Extrapolation of Eq. (S37) provides the electric intensity ( $V_f$ ) of 331.27 GV for exoelectron emission at 364 GPa near centre of Earth, provided that the relation continues to the core of Earth. Because a static mass of one electron is 0.511 MeV (=

$0.8188 \times 10^{-13}$  J), we obtain electron flux  $\xi$

$$\xi = \frac{\frac{331.27 \times 10^9}{6.2415 \times 10^{18}}}{0.8188 \times 10^{-13}} = 6.483 \times 10^5. \quad (\text{S38})$$

The flux of the electron is high enough to create sufficient number of neutral pion to trigger the fusion of deuterons. Even if the excited electrons occur in viscous Fe fluid of the outer core of Earth, the nuclear reaction could be promoted. In fact, fusion reaction  ${}^6\text{Li} (d, \alpha) {}^4\text{He}$  and  ${}^2\text{H} (d, p) {}^3\text{H}$  with  $\sim 6.83 \times 10^6$  K were measured in liquid Li acoustic (ultrasonic) cavitation.<sup>62</sup>

Neutrinos are known to be generated in the universe by the sun<sup>63</sup> or the flares of t-tauri stars<sup>64</sup> in the Archean era, and they are also produced in Earth's mantle by radioactive decay of elements, and the deuteron-thermonuclear fusion in Earth's inner core.<sup>18, 19</sup>

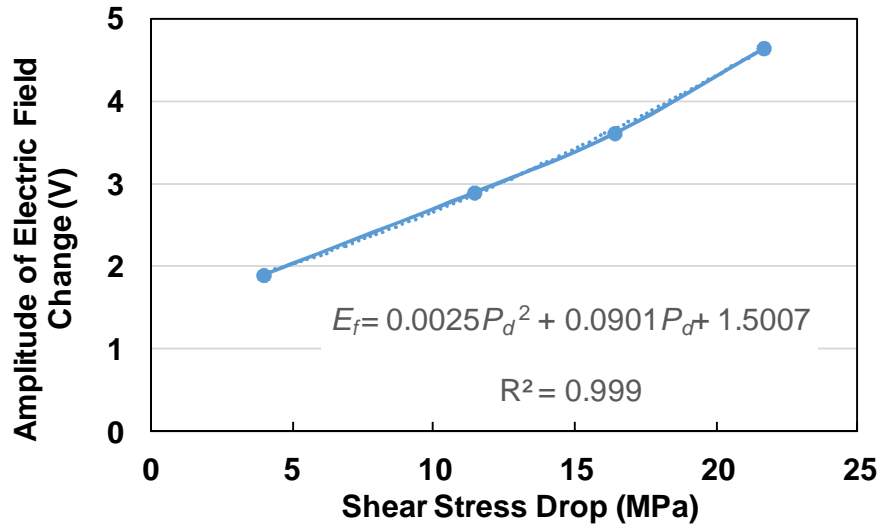


Fig. 1S. The relation between the intensity ( $V_f$ ) of the electric field signal and the magnitude ( $P_d$ ) of the stress drop for basalt sample.



#### 4. Calculation of critical temperature and pressure under confinement by high-temperature and physical catalysis effects

It is known that the pions within the nucleus allow nucleonic species to bond together and fuse with each other.<sup>65</sup> Kenny<sup>35</sup> has pointed out that attraction between deuterons could be seven times greater than in the case of nucleonic constituents thanks to pionic interactions, because pionic masses are about one-seventh that of either the proton or neutron and, thus, their interaction range is at least seven times that of their fellow nucleonic constituents based on mass alone. Since the neutral pion does not experience a Coulomb barrier,<sup>66</sup> it can easily enter within an effective nuclear force field of deuteron pairs at close proximity. We calculate a critical temperature under confinement by high-temperature and physical catalysis effects in Earth's core.

##### *(1) Confinement by the high-temperature effect*

Because the temperature at 6,378 km below the surface of Earth is reported to be about 5,700 K (Ref. 34), we considered the effect of temperature on the reaction rate  $k$ . The rate can be expressed by the Arrhenius equation:<sup>67</sup>

$$k = \frac{k_B T}{h} \frac{f_{He}^2}{f_D f_D} e^{-E/RT} \quad (S39)$$

where  $f_D$  and  $f_{He}$  are partition functions of  $^2D$  and  $^4He$ , respectively, and  $k_B$ ,  $R$  and  $E$  are the Boltzmann and Gas constants and the activation energy of the reaction, respectively.

Because  $f_D \approx f_{He}$ , we can write a ratio of the rates at temperatures  $T_0$  and  $T_1$  as follows:

$$\frac{k_1}{k_0} = \frac{T_1}{T_0} e^{\frac{E}{R} \left( \frac{T_1 - T_0}{T_0 T_1} \right)} \quad (S40)$$

With  $T_0 = 300$  K and  $T_1 = 5,700$  K, we obtain

$$\frac{k_1}{k_0} \cong 19.2. \quad (S41)$$

According to the first principle of the symmetry of force which is associated with a binding energy, the following potential form expresses the repulsive interaction between atoms:<sup>68</sup>

$$U(R) = - \frac{A}{r^{12}}, \quad (S42)$$

where  $A$  is an empirical parameter. Taking the effect of temperature on the reaction rate into consideration, we obtain a shrunken distance at 5,700 K, when radius of Fe is 0.124 nm at 300 K.

$$\begin{aligned} r_1 &\cong 0.8574 r_0 = 0.8574 \times r_0 \\ &= 0.8574 \times 0.124 \\ &= 0.10632 \text{ nm}. \end{aligned} \quad (S43)$$

## (2) Confinement by physical catalysis effect

The introduction of neutral pions makes it possible to remarkably reduce the internuclear distance between deuterons, enhancing the fusion rate for He formation, as it was physical catalysis.<sup>69</sup>

According to the Symmetrical Meson Theory of Nuclear Force<sup>68</sup> and a binding energy that tends to bosons together, we can note the interaction energy of two nucleons at separation  $r$  as follows:

$$U(R) = - \frac{C}{r^4}, \quad (S44)$$

where  $C$  is a coupling constant. Because the addition of two neutral pions (Eq.6) increases the attraction force by a factor of 14 in an interaction force of 14 times, we obtain the confinement contribution of 0.517 for D-D distance.

For the brown dwarf with an inner core of deuterium gas, furthermore, deuterium

atoms of Earth which is a rocky planet with a core of a Fe-based alloy served by the squeezing effect by 26 electrons surrounding the Fe in the tetrahedral sites of the  $\epsilon$ -Fe lattice. From Eq. (S44), we obtain the confinement effect of 0.443 for D-D distance in the latter. Thus we must use multiplied effect of physical catalysis and squeezing for calculation of  $r_2$ ,

$$r_2 \cong 0.5170 \times 0.443 \times r_o = 0.229 \times 0.124 = 0.0284 \text{ nm.} \quad (\text{S45})$$

This value would lead to fusion of D-D nuclei. Next we estimate a critical temperature corresponding to  $r_2 = 0.0284 \text{ nm}$  in Earth's core. From plotting two points (300K, 0.124 nm) and (5,700 K, 0.104 nm), we obtain a linear relation in Fig. 2Sa:

$$r = - 3.3 \times 10^{-6} T + 0.1251. \quad (\text{S46})$$

Extrapolation of Eq. (S46) provides crude estimation for the critical temperature of  $\approx 3 \times 10^4 \text{ K}$  at 0.0284 nm. In this case, we obtain  $\zeta = 1.78$   $((29,600\text{-K}/44,900\text{-K}) \times (1.0 \text{ TPa}/0.37 \text{ TPa}))$ , leading to plausible evidence for deuteron thermonuclear fusion in the Earth's core.

On the other hands, a critical pressure corresponding to  $r_2 = 0.0284 \text{ nm}$  in Earth's core gives a linear relation in Fig. S2b:

$$r = -5.508 \times 10^{-5} P + 0.1240 \quad (\text{S47})$$

Extrapolation of Eq. (S47) provides crude estimation for the critical temperature of  $\approx 1.74 \text{ TPa}$  at 0.0284 nm.

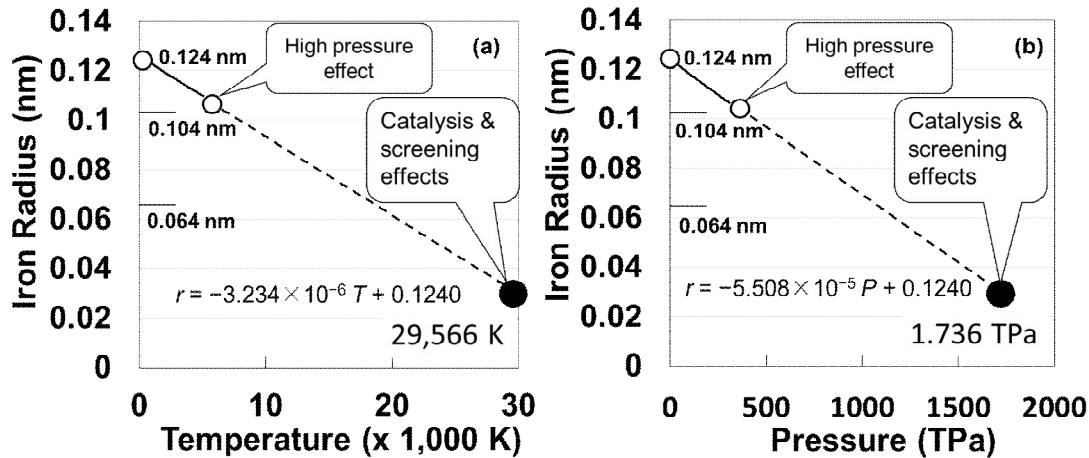


Fig. 2S Crude estimation of critical temperature (a) and pressure at center of Earth' core under confinement by high-temperature and physical catalysis effects.

**Addendum:** If we term low energy nuclear reactions “cold fusion”, we may refer Earth, Saturn, Jupiter and brown dwarfs as “warm” fusion in the image of the Sun referred as “hot” fusion.

## References

54. W. P. Allis, *Nuclear Fusion*, 1 (D. Van Norstrand Company, Princeton, 1960).
55. C. D. Van Siclen and S. E. Jones, *J. Phys. G*, **12**, 213 (1986).
56. A. Takahashi, T. Iida, and H. Miyamaru, *Fus. Tech.* **27**, 71 (1995).
57. Y. Enomoto and H. Hashimoto, *Nature (London)* **346**, 641 (1990).
58. F. T. Freund *et al.* Stimulated infrared emission from rocks: assessing a stress indicator, *eEarth Discuss*, **1**, 97 (2006).  
[www.electronic-earth-discuss.net/1/97/2006/](http://www.electronic-earth-discuss.net/1/97/2006/)
59. J. N. Brune, S. Brown, and P. A. Johnson, *Technophysics*, **218**, 59 (1993).
60. D. S. Kothari, *Proc. Royal Soc. London, Ser. A*, **165**, 486 (1938).
61. A. Tsutsumi and N. Shirai, *Tectonophysics*, **450**, 79 (2008).
62. Y. Toriabe, E. Yoshida, J. Kasagi, and M. Fukuhara, *Phys. Rev. C*, **85**, 054620 (2012).
63. L. A. McFadden and T. V. Johnson, *Encyclopedia of the Solar System*. Ed. Weissman, P. R., McFadden, L.-A. & Johnson, T. V., 68 (Academic Press, San Diego, 1999).
64. A. Unsold, *Der Neue Kosmos*, 2nd ed., 226 (Springer Verlag, Berlin, 1974).
65. S. E. Jones, S. E. *et al.* *Nature* **338**, 737 (1989).

- 66. D. F. Measday and G. A. Miller. [Ann. Rev. Nucl. Part. Sci.](#) **29**, 121 (1983).
- 67. C. Kittel, *Introduction to Solid State Physics*, sixth ed. 62 (John Wiley & Sons, New York, 1986).
- 68. R. T. Bush and R. D. Eagleton, [J. Fus. Ener.](#) **9**, 397 (1990).
- 69. M. Fukuhara, [Fus. Sci. Tech.](#) **43**, 128 (2003).