

Inertial Confinement of Fusion Plasma

It has taken over 60 years of ICF development to achieve the current state of NIF [J.D. Lindl, 1998, *Inertial Confinement Fusion*, p. 16].

As of September 2012, NIF had cost over \$5 billion [www.nytimes.com/2012/09/30/science/fusion-project-faces-a-frugal-congress.html], not counting earlier ICF machines and research.

What is the true total cost of NIF now? ~\$10 billion? [current annual cost ~\$0.624 billion, www.llnl.gov/news/national-ignition-facility-achieves-fusion-ignition]

Compared to NIF, a power plant would need to increase:

- Gain by ~3 orders of magnitude
- Fusion energy output per day by ~8 orders of magnitude

AND

How much would such a power plant cost?

How complex would such a power plant be?

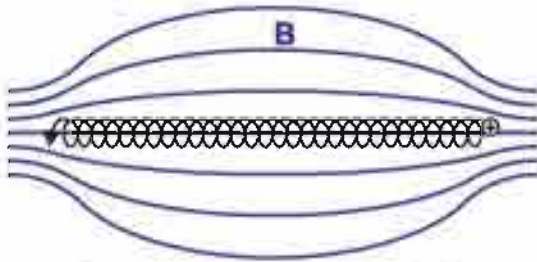
How many more decades would be required to achieve that goal?

Why would electric utility companies buy many ICF power plants like that instead of cheaper, simpler, more readily available renewable, fission, or fossil fuel plants?

The most justifiable use of NIF may be as a “wind tunnel” for subscale modeling of nuclear weapons, astrophysical processes, etc., and as a WPA project to retain enough scientists/engineers with expertise relevant to nuclear weapons.

Magnetic Confinement of Fusion Plasma

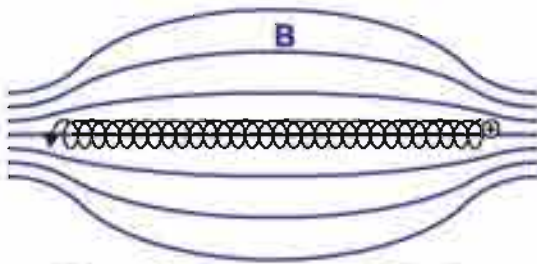
Charged particles spiraling along magnetic field lines B cannot easily cross them to escape



Problem 1: Large particle losses at ends, even with magnetic mirrors, electrostatic plugs, etc.

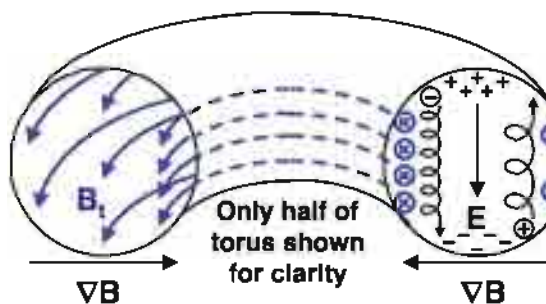
Magnetic Confinement of Fusion Plasma

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Problem 1: Large particle losses at ends, even with magnetic mirrors, electrostatic plugs, etc.

Solution 1:
Eliminate the ends by bending lines into a closed toroidal field B_t

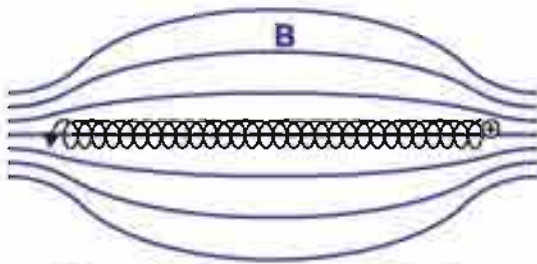


Problem 2:
 ∇B & $E \times B$ drifts together let particles escape

$E \times B$ drift

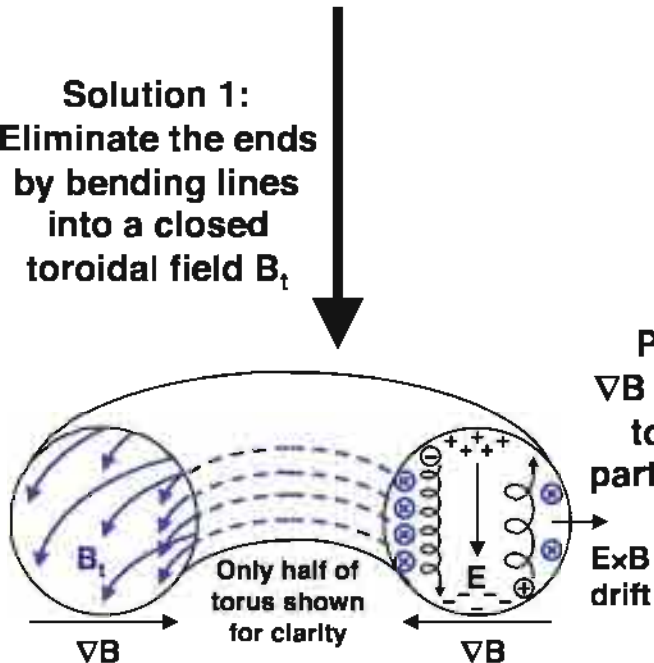
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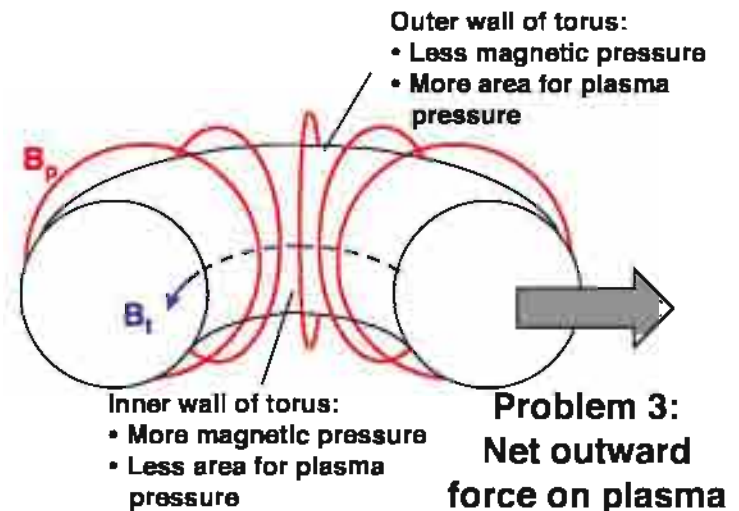
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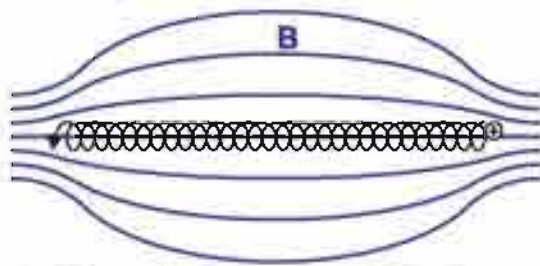
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Solution 2: Add poloidal field B_p to mix particles in inner and outer regions of torus



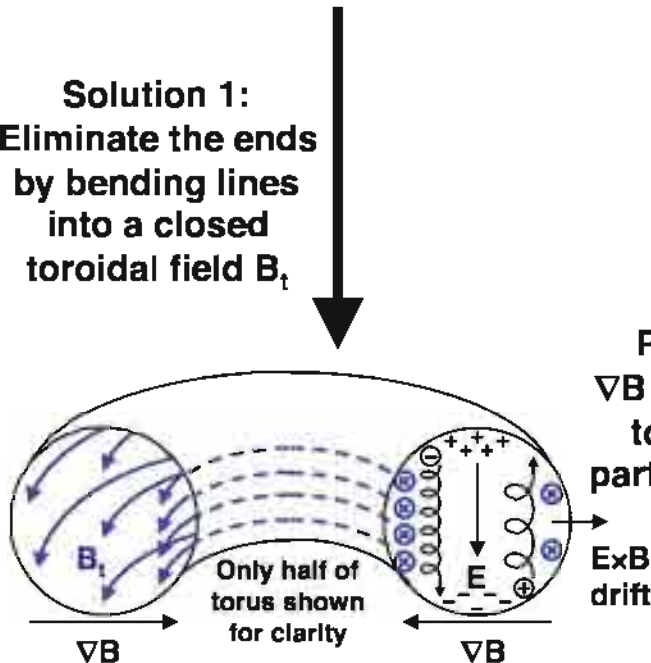
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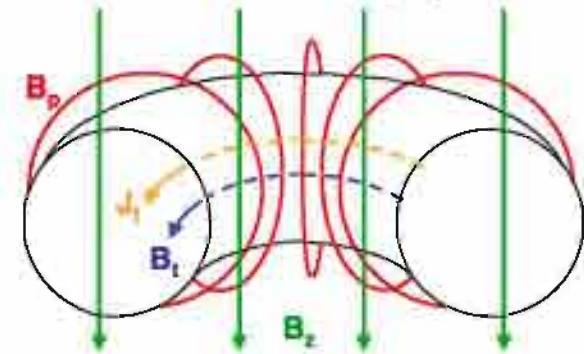
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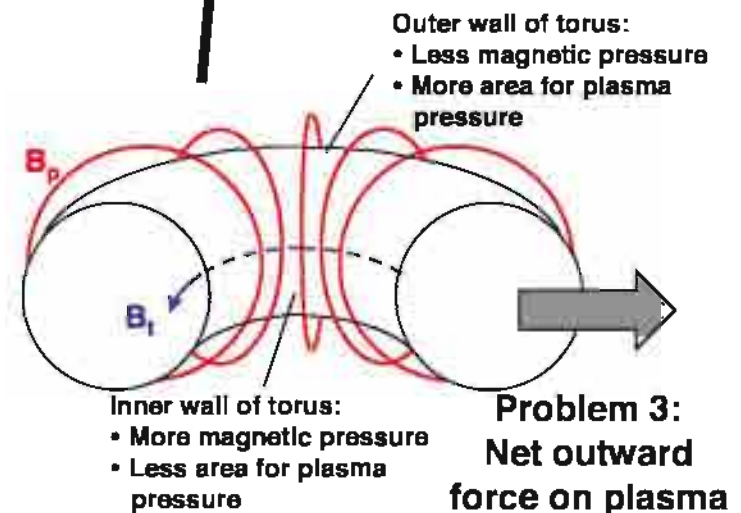
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Tokamaks, stellarators, RFPs, FRCs, etc. differ in how they create the plasma current and B_t , B_p , & B_z

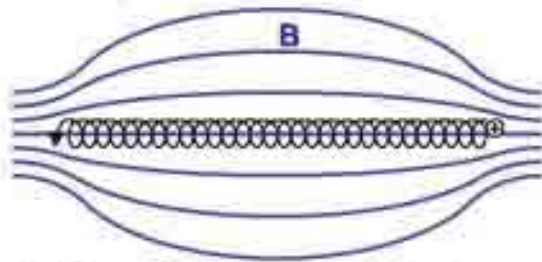


Solution 3: Add vertical field B_z that acts on toroidal current J_t to balance outward forces on plasma



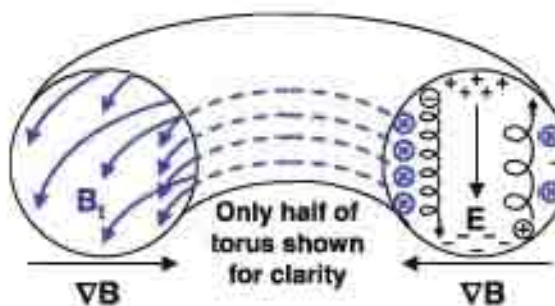
Magnetic Confinement of Fusion Plasma

Charged particles spiraling along magnetic field lines B cannot easily cross them to escape



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Goals (somewhat conflicting):

Maximize β = plasma pressure / magnetic pressure

Minimize B inside plasma to avoid cyclotron radiation losses

Maximize fusion power density to minimize hardware cost

Inner hardware subject to radiation damage is inexpensive and easily accessible

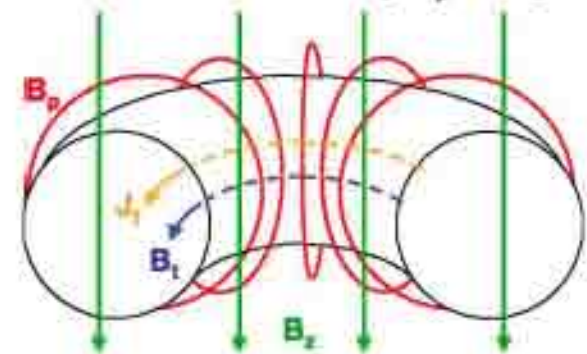
Confine fuel ions and electrons but let charged products escape

Provide for lithium-6 blanket if necessary

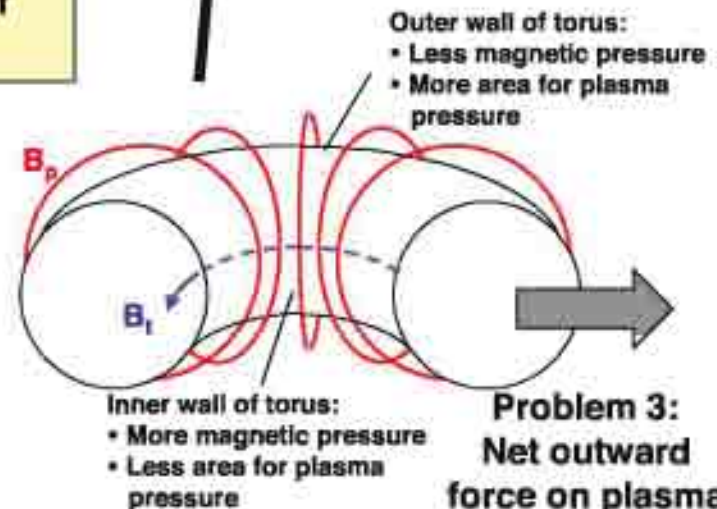
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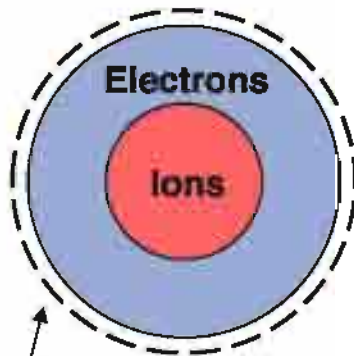
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Problem 3:
Net outward force on plasma

Other Confinement of Fusion Plasmas (1)

Electrostatic



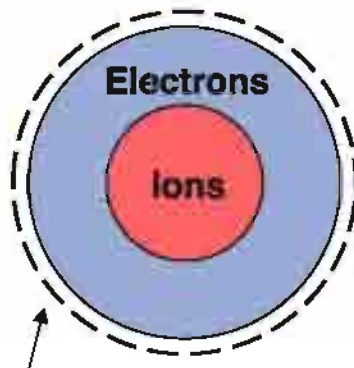
High-voltage grid
or polyhedral cusp
magnetic field

- Electron potential well confines ions but ion upscattering losses are prohibitive
- Grid or cusp field confines electrons but electron losses are prohibitive

T.H. Rider 1995,
Phys. Plasmas 2:1853 & 1873

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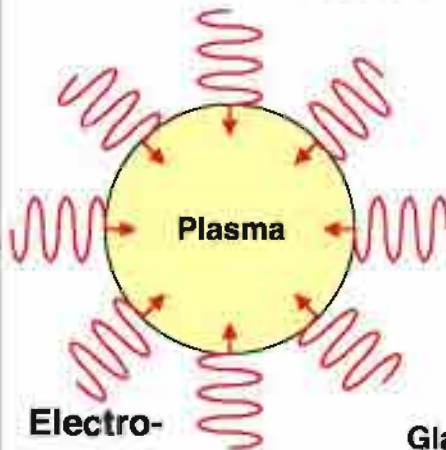


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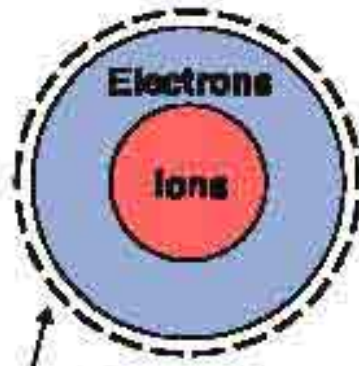
Electro-
magnetic
waves

- Electromagnetic wave pressure confines plasma
- Power Input is prohibitive

Glasstone & Lovberg 1960,
Controlled Thermonuclear Reactions,
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Acoustic: So No Fusion

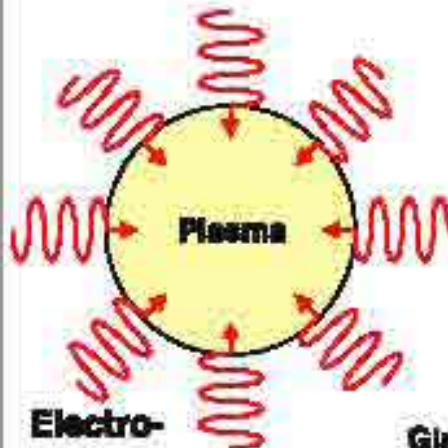
Acoustic waves in deuterated acetone



- Acoustic waves in the acetone compress bubbles to fusion conditions???
Not replicated!
- Thermal conduction losses from heated region to surrounding liquid are prohibitive

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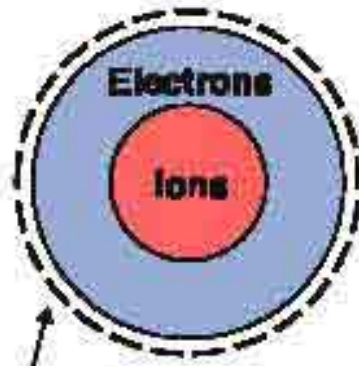
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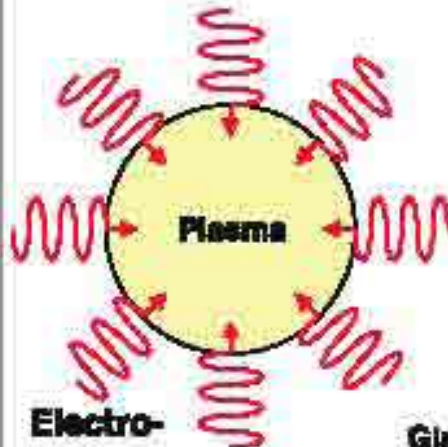
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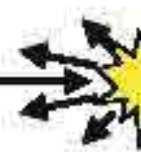
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Beam + Solid Target

Tritons or
other particles
or laser beam



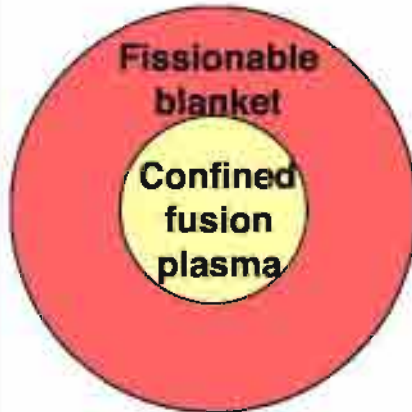
Solid
deuterium
target or
other fuel

- Electrons in the target absorb and conduct away far too much of the beam energy for breakeven

Glasstone & Lovberg 1960, *Controlled Thermonuclear Reactions*, Van Nostrand, pp. 64-66

Other Confinement of Fusion Plasmas (2)

Fusion-Fission Hybrid

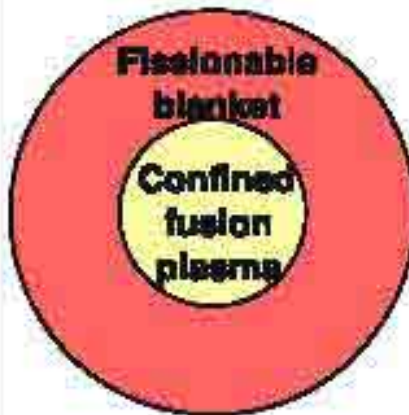


Has disadvantages of both fusion & fission:

- Fusion plasma requires expensive and complicated confinement system
- Fission blanket creates radioactive fission products and actinide waste
- Hybrid ICF pellets would blast fission products all over the target chamber

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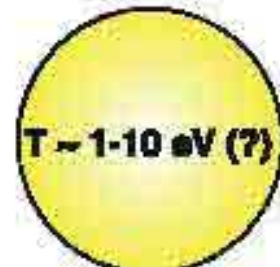


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Ball Lightning

Observed
lifetime > 2-5 sec



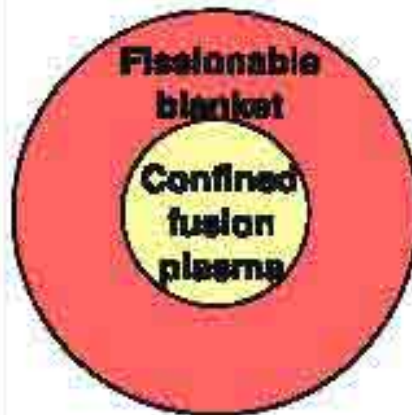
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- What is the confinement mechanism, especially in view of the virial theorem?
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Mark Stenhoff 1999, *Ball Lightning*, Kluwer/Plenum
K.H. Tsui 2003, *Phys. Plasmas* 10:4112

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Small Black Hole

Compresses and heats matter to fusion conditions before it reaches the event horizon

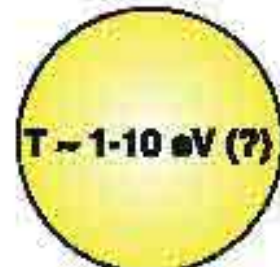


- No signs of natural small black holes in our solar system
- Creating a black hole via implosion is orders of magnitude more challenging than even ICF

L.L. Wood et al 1975, *Annals NY Acad. Sci.* 261:823

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$T \sim 1-10 \text{ eV (?)}$

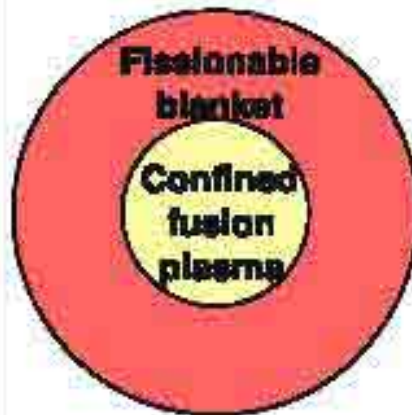
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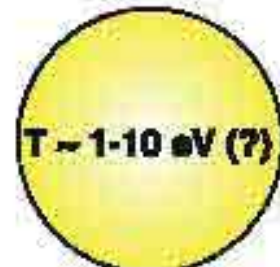


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- Are there other confinement approaches?
- Can one show that these ideas completely cover the phase space of confinement approaches?

Conversion to Electrical Energy

Heat

Carnot limit:

$$\text{Efficiency} < 1 - \frac{T_{\min}}{T_{\max}}$$

$$\sim 0.3 - 0.4$$

for $T_{\min} \sim 300^\circ\text{K}$, $T_{\max} \sim 500^\circ\text{K}$
(before something melts)

- Conventional methods add moving parts and fluids
- Thermoelectric conversion
- Thermoacoustic conversion

Conversion to Electrical Energy

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Fundamental Constraints on Fusion Approaches

(Barring Miracles—Wait One Slide...)

Fusion approaches that do not appear suitable for practical power-producing reactors:

- Nonmagnetic confinement (inertial, electrostatic, electromagnetic, and acoustic), excluding stars and bombs
- Plasma systems operating substantially out of thermodynamic equilibrium
- Advanced aneutronic fuels ($^3\text{He}+^3\text{He}$, $p+^{11}\text{B}$, $p+^6\text{Li}$, etc.)
- Most high-efficiency direct electric converters

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Best foreseeable 1 GW_e (3 GW_t) magnetic fusion reactors:

- D+T: 2.4 GW of 14-MeV neutrons, 1.6 giga-Curies (G Ci) of T stockpile/year
- D+D w/o product burnup: 1 GW 2.5-MeV neutrons, 1 GW X-rays, 70 G Ci T
- D+D with product burnup: 1.1 GW mainly 14-MeV neutrons, 180 MW X-rays
- D+ ^3He w/o product burnup: 30 MW 2.5-MeV neutrons, 500 MW X-rays, 1.8 G Ci T
- D+ ^3He with product burnup: 150 MW mainly 14-MeV neutrons, 500 MW X-rays
- Mainly thermal (Carnot-limited) conversion of fusion energy to electricity

Potential Thesis (or Nobel Prize) Topics

Fusion reactions:

- In the table of possible fusion reactions, should additional reactions be green?
(Consider competing side reactions and idealized breakeven against bremsstrahlung.)
- Are there any promising reactions not in the table (due to higher Z or shorter nuclide half-life)?

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- Benefits of spin-polarized fusion (especially for D+D reaction enhancement or suppression).
- Methods of producing polarized nuclei.
- Mechanisms and rates of depolarization relative to the fusion rate.

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Other ways to improve the tunneling factor:

- Is there a way to keep scattering from hindering shape-polarized fusion?
- Is the resonant tunneling model valid, and does it have useful consequences?
- Is fusion of light elements in liquid metallic states scientifically valid and practical to achieve?
- Are there other ways to improve the tunneling factor?
- Can one prove we have covered the complete phase space of ideas for improving the tunneling factor?

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Other improvements to σ_{fus} :

- Are there ways to improve the wavefunction cross-sectional area factor in σ_{fus} ?
- Are there ways to improve the Breit-Wigner compound nucleus energy resonance factor in σ_{fus} ?
- Are there any other categories of ways to influence σ_{fus} ?

More Potential Thesis (or Nobel Prize) Topics

Fusion products:

- Are there practical ways to influence the reaction channels and products?

More Potential Thesis (or Nobel Prize) Topics

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- Are there practical ways to influence the reaction channels and products?

Plasma properties:

- Are there realistic ways to recirculate power and maintain ions in a monoenergetic or anisotropic state, or two ion species at different temperatures (e.g. hot ^3He and cold D or hot p^+ and cold ^{11}B)?
- Are there practical ways to reduce ion-electron energy transfer or recirculate power from the electrons back to the ions?
- Are there ways to reduce and/or convert radiation power losses, especially bremsstrahlung?

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Confinement of particles and energy:

- Are there practical lessons we can learn from stellar fusion and use to improve fusion reactors?
- Are there ways to overcome the main practical difficulties with inertial confinement fusion?
- Which existing magnetic confinement approach is best, or can a better one be created?
- Can the conduction losses be reduced to make acoustic confinement practical?
- Can fusion-fission hybrids be made more attractive?
- How is ball lightning confined, and can fusion reactors employ a similar approach?
- Is there any feasible way to create a small black hole?
- Are there any other confinement approaches worthy of investigation?

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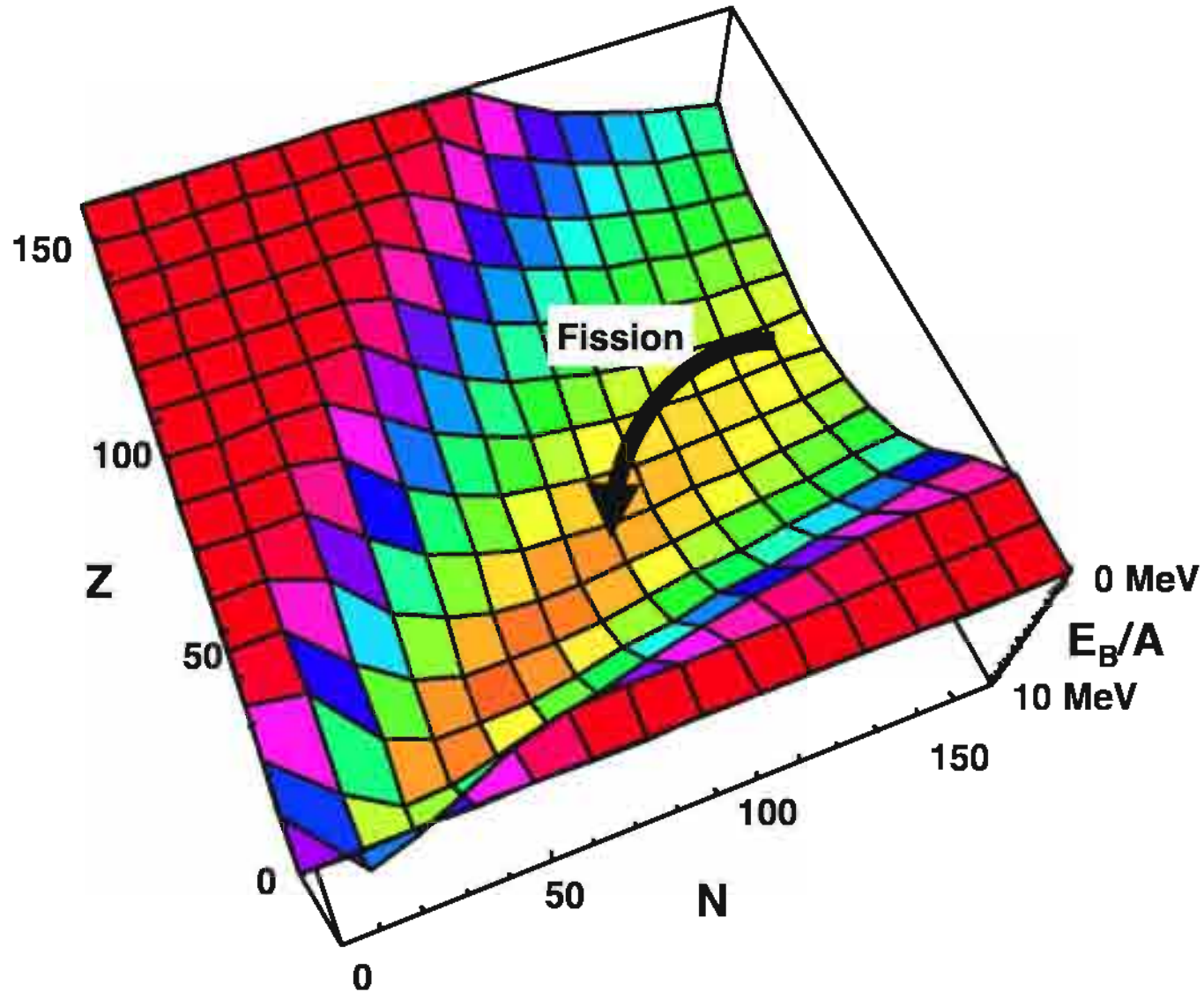
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Conversion to electrical energy:

- What are the most efficient and/or most compact thermal-to-electric converters?
- What are the best converters for light nuclei—inverse linear accelerators, inverse cyclotrons, etc.?
- Are there practical ways to directly convert the energies of recoil nuclei or other heavy nuclei emitted by solid materials?
- What are the best converters for electrons?
- How practical and efficient can neutron energy conversion methods be [Perkins 1986, 1988]?
- How practical and efficient can X-ray and γ -ray energy conversion methods be [Weaver 1973]?

Binding Energy per Nucleon And Methods of Tapping It



Fission Process

$$\frac{E_{\text{Coulomb}}}{E_{\text{surface}}} \propto \frac{Z^2}{A} \sim 0.4 \frac{Z}{A} \text{ for heavy nuclei}$$

Fission barrier height:

$$V_B \sim 9 A^{2/3} [1 - (Z^2/A)/49] \text{ MeV}$$

$$+ \begin{cases} 0.3 \text{ MeV} & \text{if odd-odd} \\ 0 \text{ MeV} & \text{if odd-even} \\ -0.3 \text{ MeV} & \text{if even-even} \end{cases}$$

+ shell corrections

~ 5.6 MeV for even U/Pu isotopes

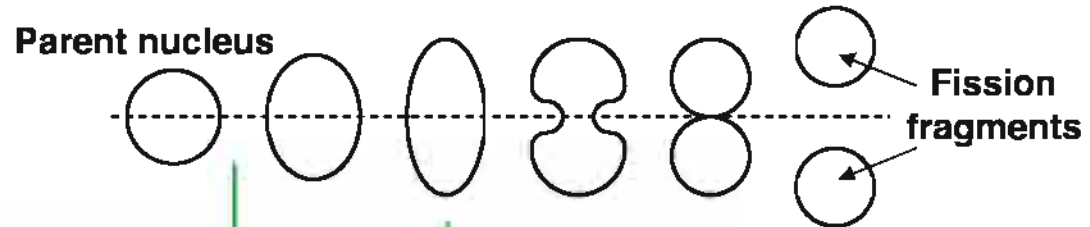
~ 6.2 MeV for odd U/Pu isotopes

Captured neutron adds energy to nucleus:

~ 5 MeV for even U/Pu compound nucleus

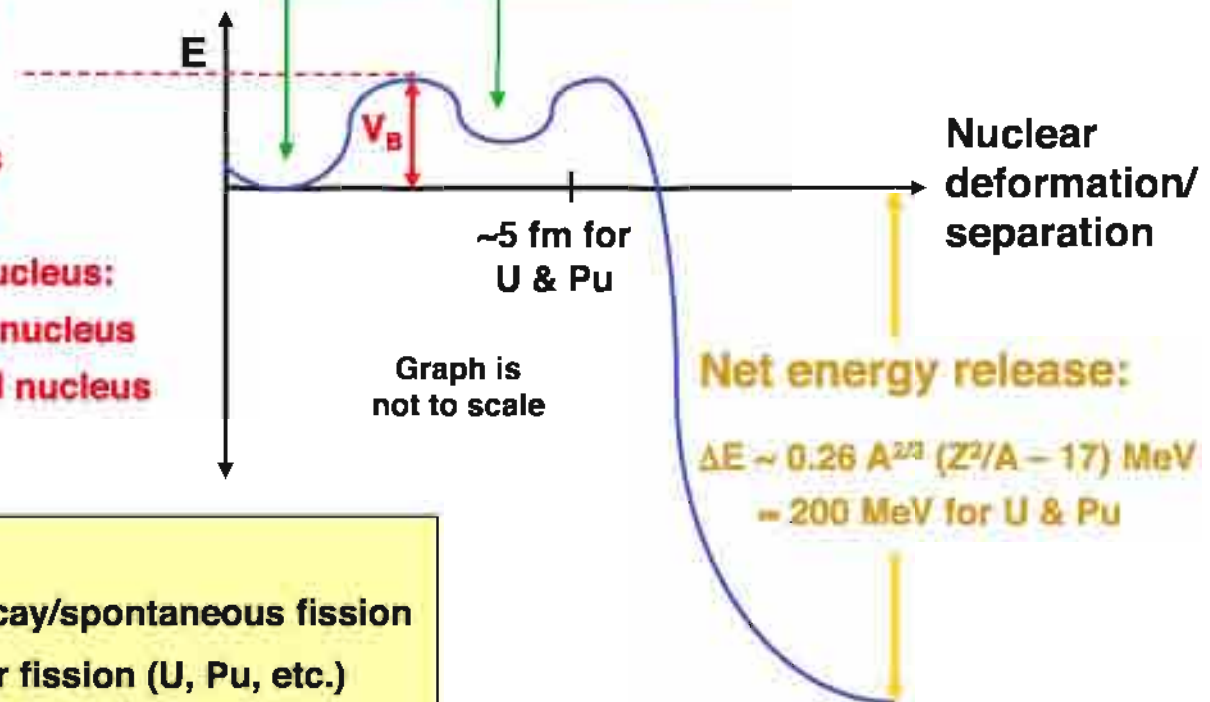
~ 6.5 MeV for even-odd compound nucleus

Parent nucleus



Ground state of heavy nucleus is slightly deformed due to shell effects

Valley in barrier due to shell effects (fission isomers with ~ns half-lives)



- $Z < 90$: barrier too high for fission
- $Z > 96$: barrier too low; rapid α decay/spontaneous fission
- Even- Z nuclei generally better for fission (U, Pu, etc.)
- Odd- N target nuclei generally better for n-induced fission (^{235}U vs. ^{238}U , etc.)

Fission Fuels and Sources

Energy Production

Only 3 natural actinide resources:

^{235}U

- Directly useful as fuel
- Naturally mixed with ^{238}U
- $>3 \times 10^8$ kg readily accessible to mining
 - $>3 \times 10^5$ GWe-years (1/3 thermal effic.)
 - >15 years of present global energy consumption rate

^{238}U

- Transmute to ^{239}Pu fuel in breeder reactor
($n + ^{238}\text{U} \rightarrow ^{239}\text{U} \xrightarrow{\beta} ^{239}\text{Np} \xrightarrow{\beta} ^{239}\text{Pu}$)
- $>4 \times 10^{10}$ kg readily accessible to mining
 - $>4 \times 10^7$ GWe-years
 - >2000 years of global consumption

^{232}Th

- Transmute to ^{233}U fuel in breeder reactor
($n + ^{232}\text{Th} \rightarrow ^{233}\text{Th} \xrightarrow{\beta} ^{233}\text{Pa} \xrightarrow{\beta} ^{233}\text{U}$)
- $>8 \times 10^9$ kg readily accessible to mining
 - $>8 \times 10^6$ GWe-years
 - >400 years of global consumption

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Energy Storage

Most fissile isotopes that can be artificially produced:

$^{242\text{m}}\text{Am}$

- Critical mass ~ 23 g dispersed in water
- 141-year half-life
- Small quantities produced in U or Pu reactors; final step is $^{241}\text{Am}(n,\gamma)^{242\text{m}}\text{Am}$

^{245}Cm

- Critical mass ~ 47 g dispersed in water
- 8500-year half-life
- Small quantities produced in U or Pu reactors

^{254}Cf

- Spontaneous fission dominates decay
- 60.5-day half-life
- Minute quantities produced in reactors

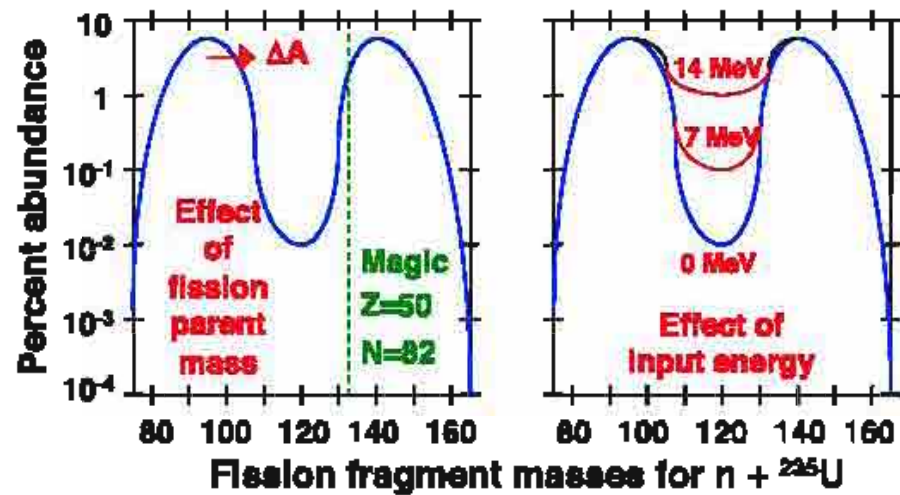
Anderson 1989, *A Physicist's Desk Reference*, AIP. www.lea.org. yearbook.enerdata.net. www.world-nuclear.org.

Anno et al 2003, Actinides Critical Masses and the Paxton Woodcock Rule, *Proc. ICNC 2003*:71.

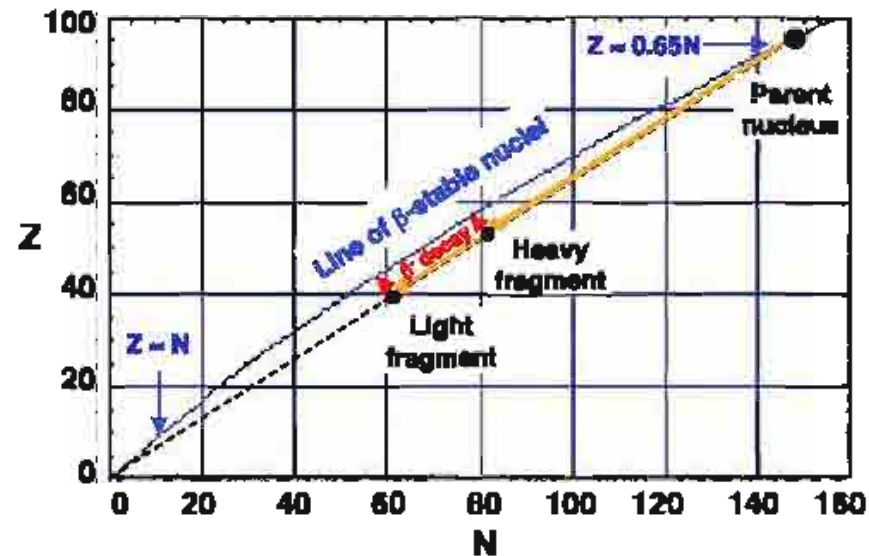
Fission Waste Production

Fission fragments

Asymmetric & wide range of fragments



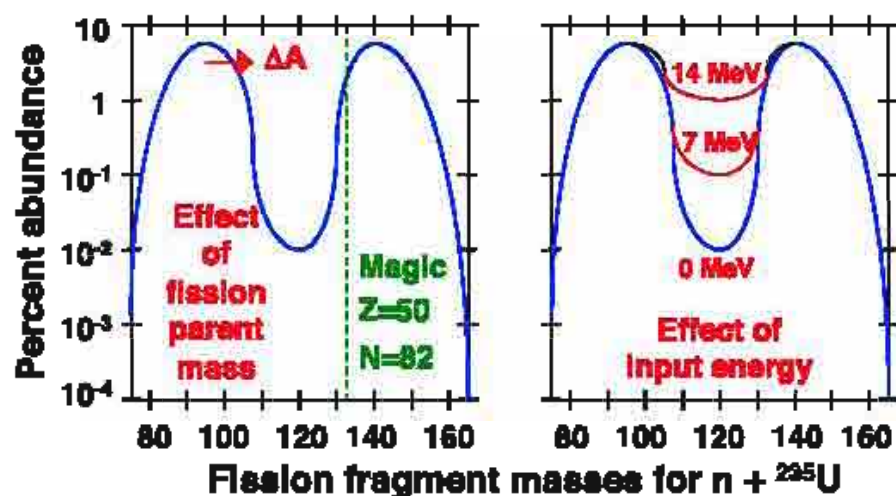
Fragments must be β^- emitters



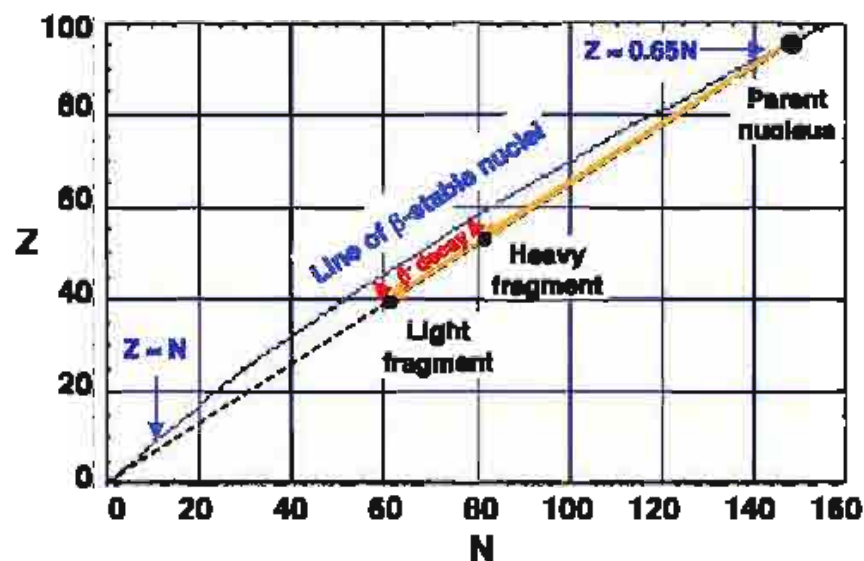
Fission Waste Production

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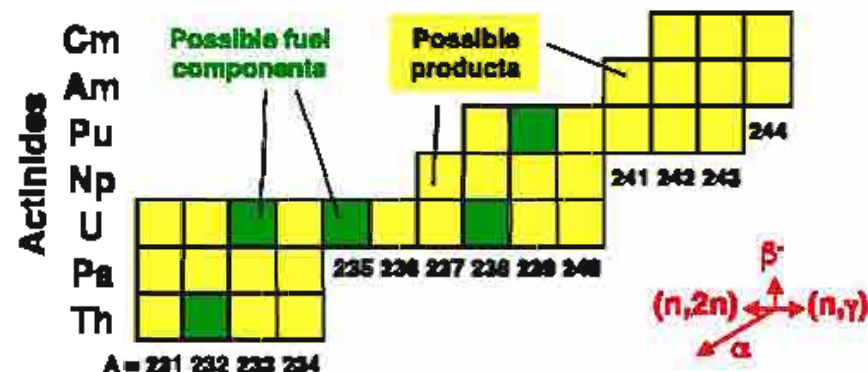
Asymmetric & wide range of fragments



Fragments must be β^- emitters



Neutron activation within fuel

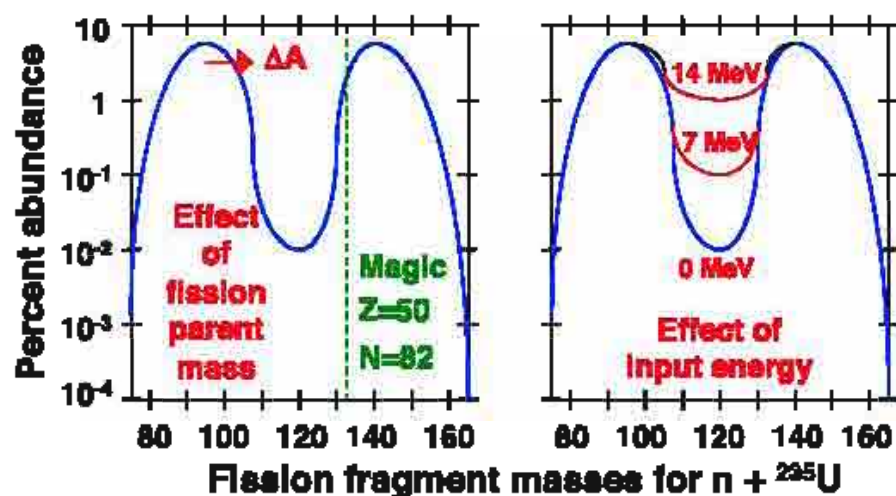


- Few choices for fissile fuel to control products
- Eliminating other actinides from fresh fuel reduces waste but makes fuel a proliferation & criticality hazard and also prevents breeding

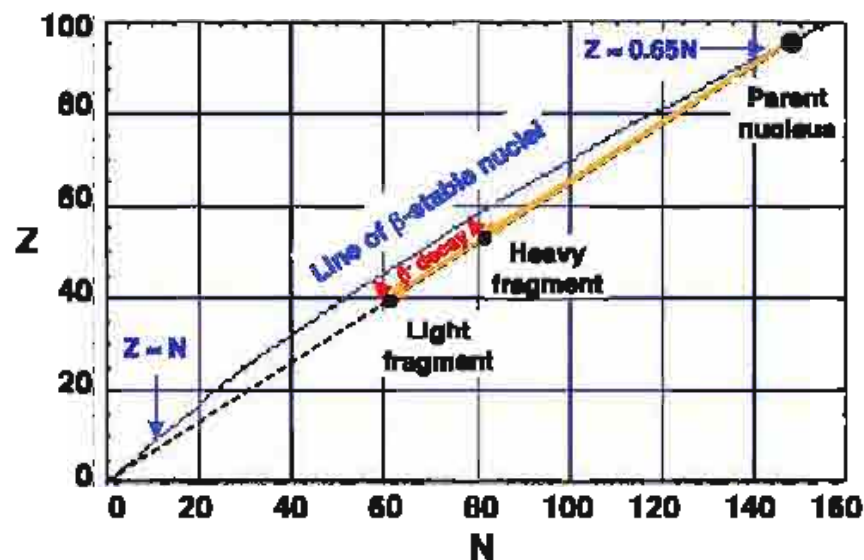
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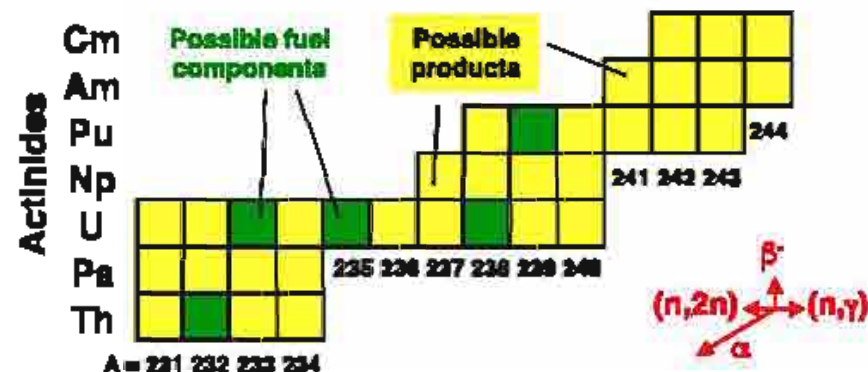
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Fragments must be β^- emitters



Neutron activation within fuel



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Other neutron activation

Low-activation materials

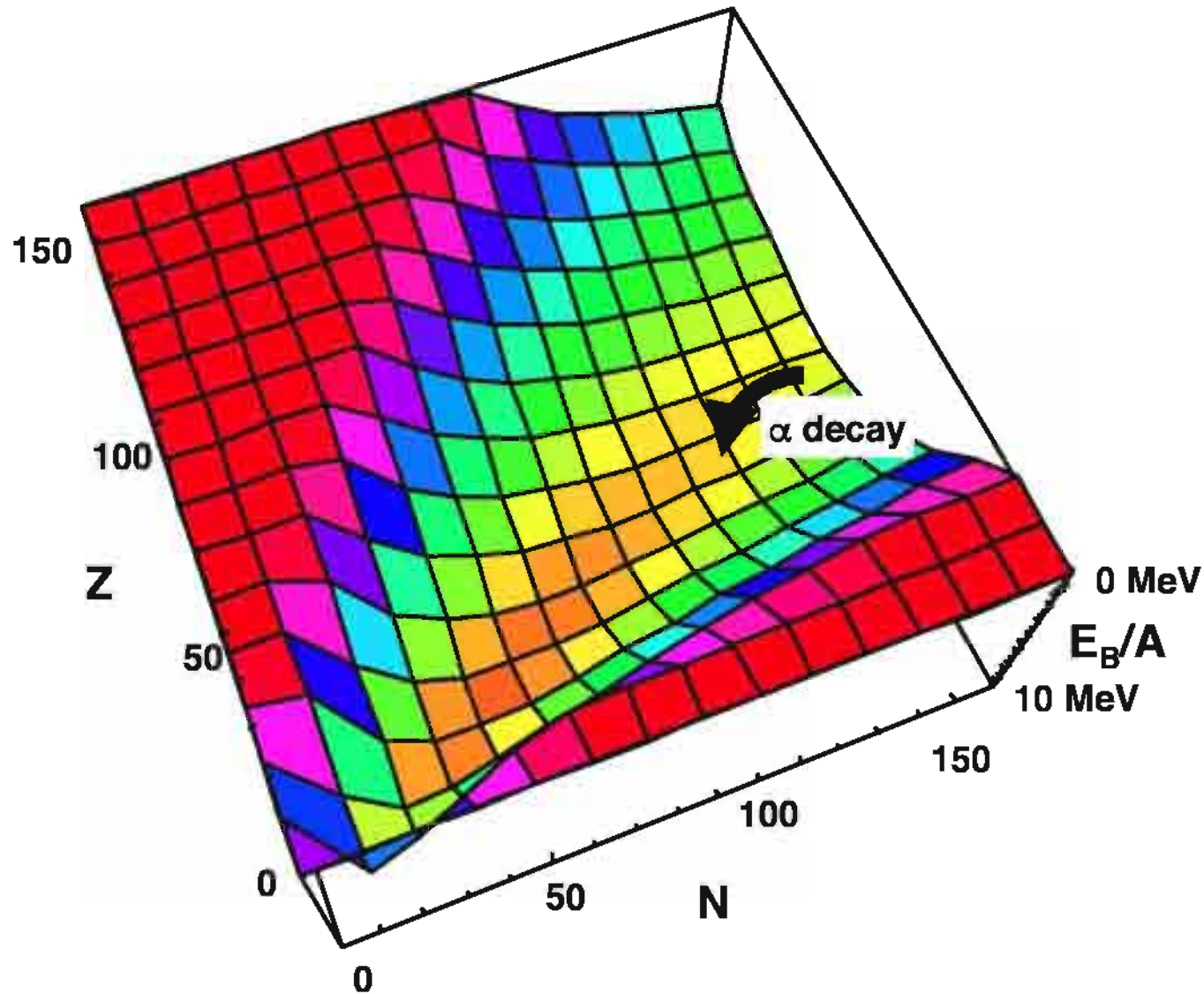
Moderators:	H_2O , D_2O , ${}^{12}\text{C}$, etc.
Coolants:	H_2O , D_2O , ${}^{23}\text{Na}$, etc.
Control rods:	${}^{10}\text{B}$, ${}^{11}\text{B}$, ${}^{13}\text{C}$, etc.
Reflectors:	${}^9\text{Be}$, ${}^{12}\text{C}$, etc.
Structural metals:	${}^{94}\text{Zr}$, ${}^{96}\text{Mo}$, etc.

- Some tritium is produced by D_2O , ${}^{10}\text{B}$, etc.
- Still room for improvement in low-cost, high-temperature alloys that minimize activation or embrittlement by neutrons

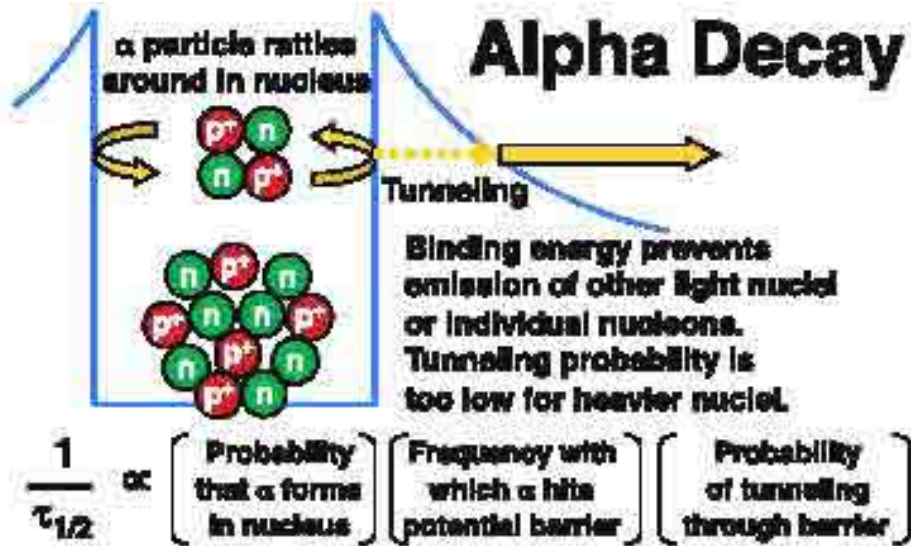
Fission Power

- **Are there any ways to intervene at the nuclear level to make the fission process cleaner, easier, or better?**
- **What are the best sources and methods for obtaining fission fuel?**
- **What are the best materials to use in fission reactors?**
- **What are the safest, cheapest reactor designs for using fission fuel?**
- **What are the most efficient methods for converting fission energy to electrical energy? (Convert fission fragment K.E. to electric energy?)**
- **What are the most efficient methods for harnessing fission energy for rocket propulsion?**
- **What are the best ways of separating/reusing/burning up/storing waste?**
- **What are the best ways to make fission reactors resistant to accidents, terrorism, nuclear weapons proliferation, etc.?**

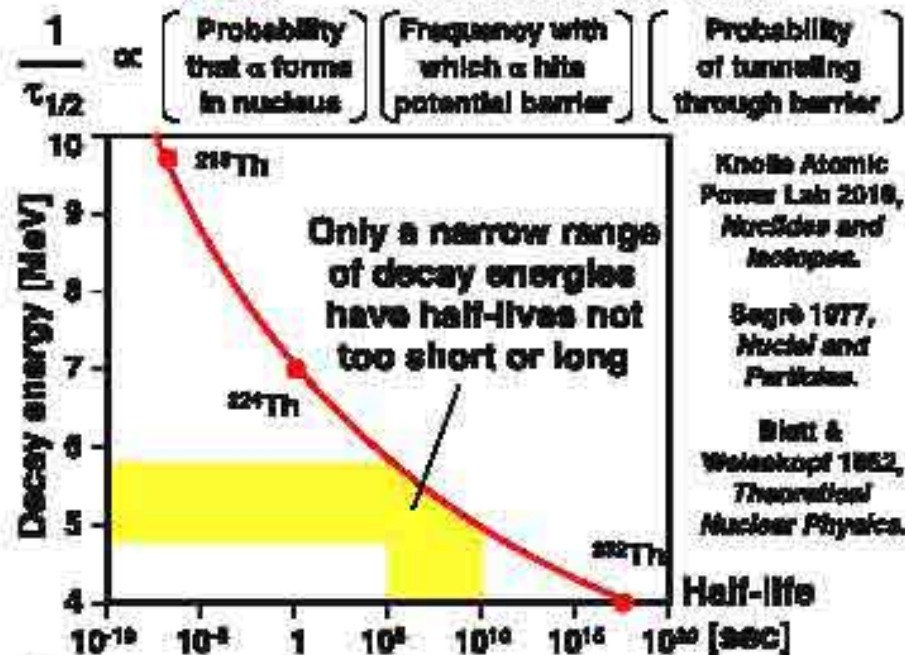
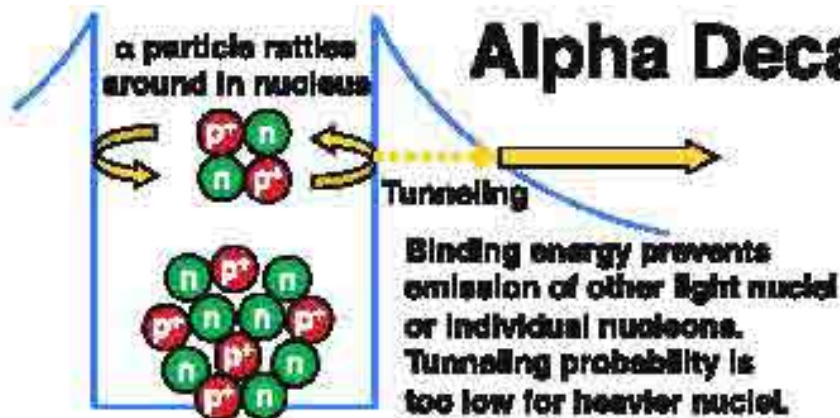
Binding Energy per Nucleon And Methods of Tapping It



Alpha Decay



Alpha Decay



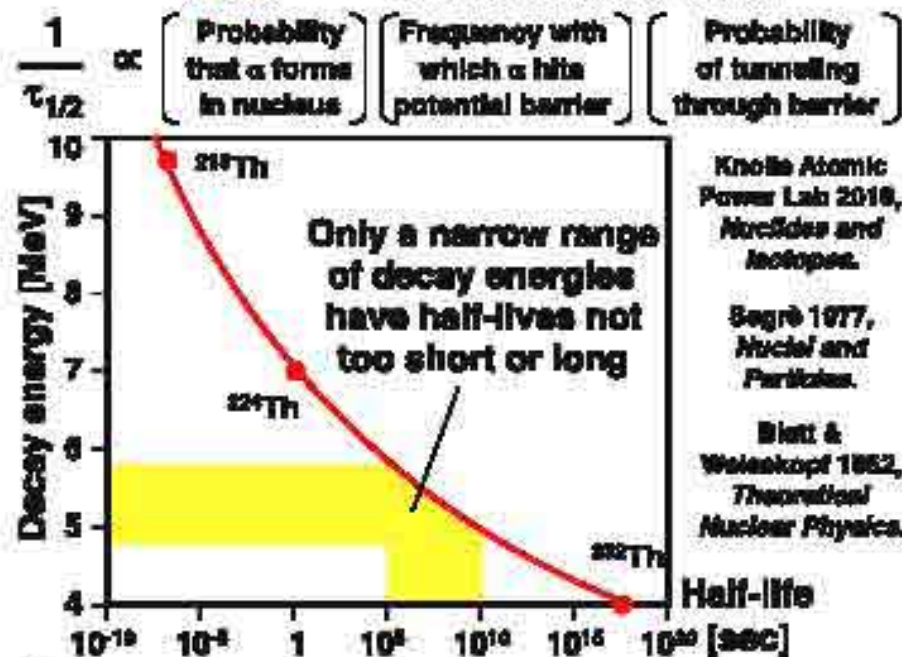
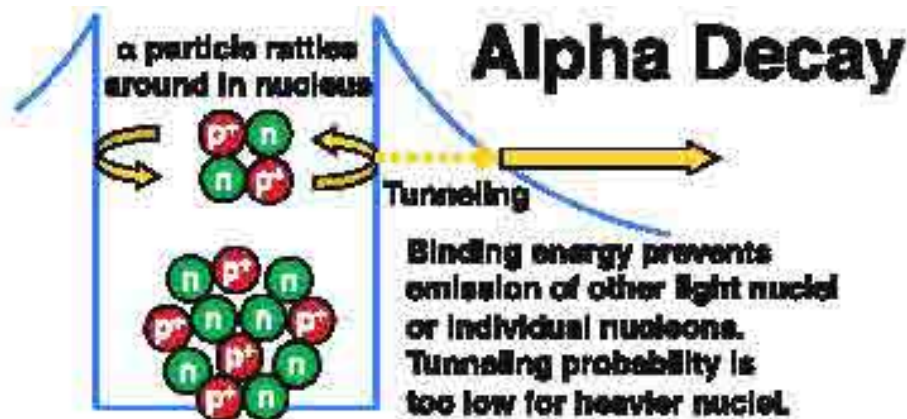
Knoles Atomic Power Lab 2010, *Nuclides and Isotopes*.

Segrè 1977, *Nuclei and Particles*.

Blatt & Weisskopf 1952, *Theoretical Nuclear Physics*.

Some α emitters

Nucleus	Energy	Half-life	Initial power
²¹⁰ Po	5.3 MeV	136 days	141 W/g
²⁴² Cm	6.1 MeV	163 days	120 W/g
²⁴⁴ Cm	5.8 MeV	18.1 yrs	2.84 W/g
²³⁸ Pu	5.5 MeV	88 yrs	0.68 W/g
²⁴¹ Am	5.5 MeV	432 yrs	0.11 W/g

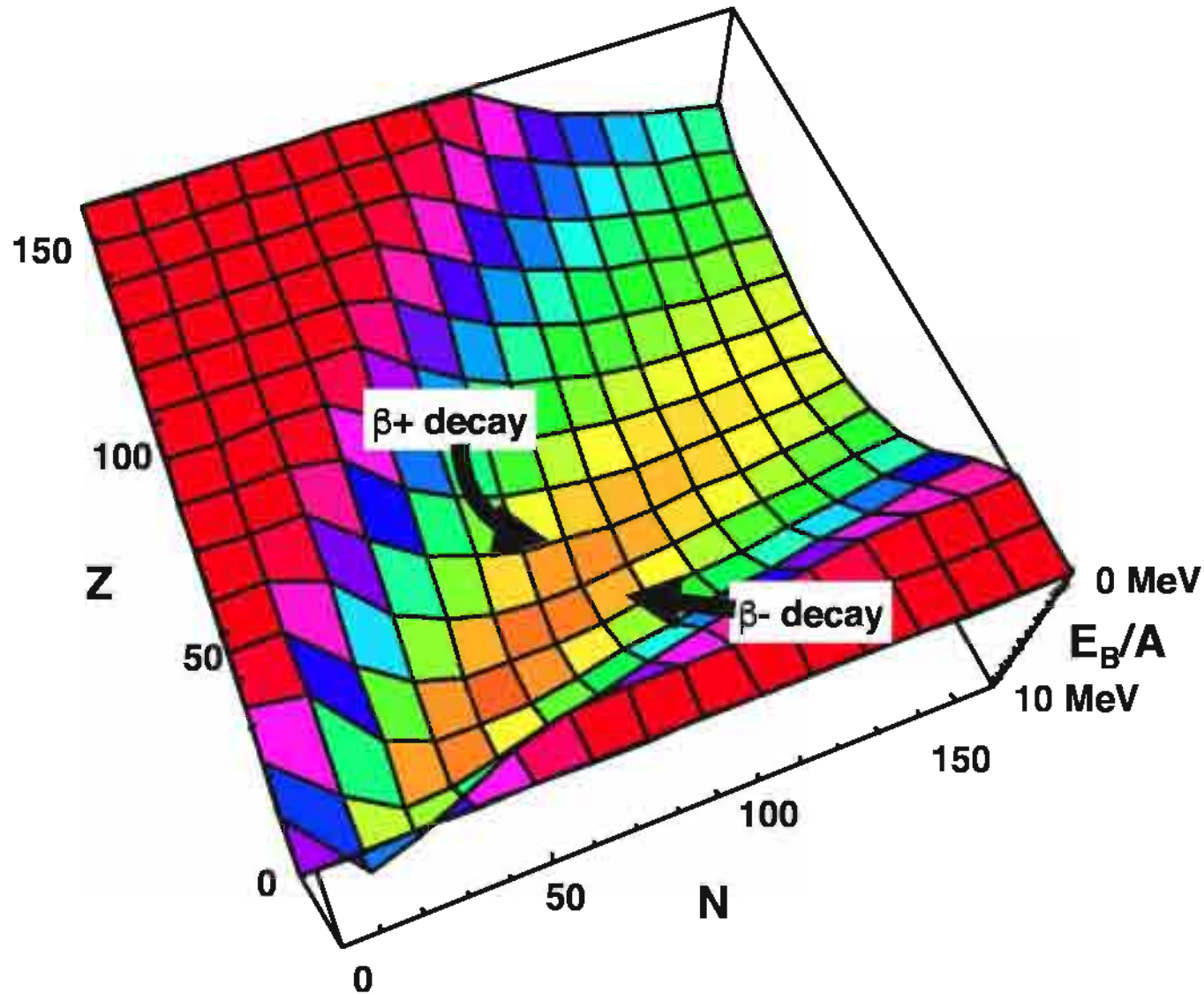


Some α emitters

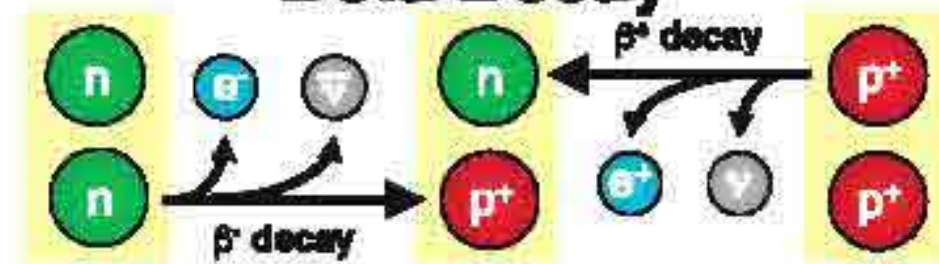
Nucleus	Energy	Half-life	Initial power
^{210}Po	5.3 MeV	136 days	141 W/g
^{242}Cm	6.1 MeV	163 days	120 W/g
^{244}Cm	5.8 MeV	18.1 yrs	2.84 W/g
^{238}Pu	5.5 MeV	88 yrs	0.58 W/g
^{241}Am	5.5 MeV	432 yrs	0.11 W/g

- Are there practical ways to use similar processes to make nuclei emit particles other than α particles (or β or γ)?
- Are there any α emitters that are easier to produce and/or easier to use than those in the table?
- Are there any ways to suppress the rate of α decay when it is not desired (e.g., to keep energy stored during a long interplanetary trip) and/or induce α decay when it is desired (e.g., when especially large amounts of output power are needed during an interplanetary mission)?
 - Difficult to alter potential without \sim MeV input energies.
 - Nearby negative charges to decrease Coulomb barrier?
 - Nearby positive charges to increase Coulomb barrier?
 - Strong fields—electric, magnetic, electromagnetic, etc.?
 - Any practical ways to alter the shape of the nucleus?
 - Nuclear capture of a neutron, electron, antiproton, etc.?
 - Temporarily loan energy to the nucleus then recover it?
- Are there better methods to convert the kinetic energy of the α particles and the emitting nuclei to electricity?
 - Nonthermal conversion challenging: \sim μm range of alphas.
 - Increase Seebeck thermoelectric conversion efficiency?
 - Increase thermionic converter efficiency?
 - Increase thermophotovoltaic converter efficiency?
 - Get hot enough for Stirling engines, gas turbines, etc.?
 - Particle conversion and/or energy amplification by combining with other nuclear processes/materials?
 - Electrostatic converters, inverse ion accelerators, etc.?
 - Are there other methods of conversion?
 - Multiple conversion methods to maximize efficiency?
- Are there effective and practical ways to convert the kinetic energy of the alpha particles and the emitting nuclei to the kinetic energy of rocket exhaust?

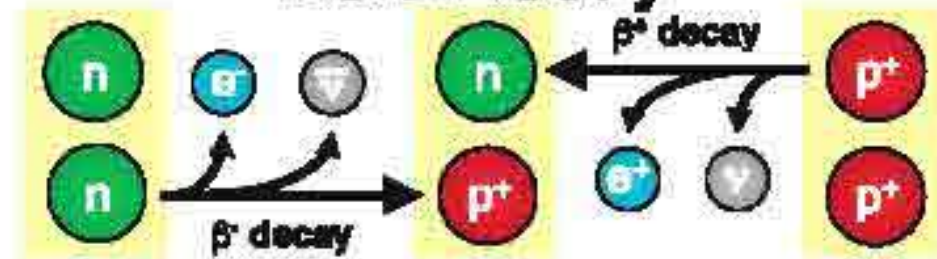
Binding Energy per Nucleon And Methods of Tapping It



Beta Decay



Beta Decay



$$\tau_{1/2} \propto (10^4)^L (\Delta E)^{-4}$$

Some β emitters of interest

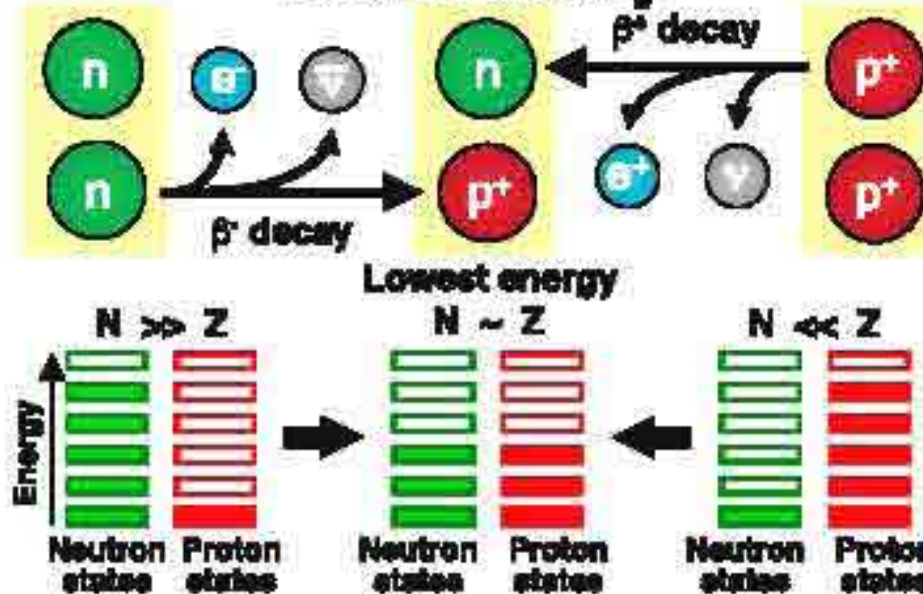
Nucleus	Energy	Half-life	Initial power
¹⁰⁶ Ru	39.4 keV	1.02 yr	31.8 W/g
¹⁴⁴ Ce	318 keV	285 days	25.5 W/g
¹⁰⁶ Co	318 keV	5.3 yr	17.5 W/g
¹⁷⁰ Tm	968 keV	129 days	11.9 W/g
⁹⁰ Sr	548 keV	29.1 yr	0.92 W/g
⁸⁶ Kr	687 keV	10.7 yr	0.59 W/g
¹³⁷ Cs	514 keV	30.2 yr	0.43 W/g
¹⁴⁷ Pm	224 keV	2.52 yr	0.34 W/g
³ H	18.6 keV	12.3 yr	0.33 W/g

Initial powers include daughter reactions: Knoll's Atomic

Power Lab 2010, Nuclides and Isotopes: Chart of the Nuclides.

Blatt & Weisskopf 1952, Theoretical Nuclear Physics, Segrè 1977, Nuclear and Particle, DeGroot & Feshbach 1974, Theoretical Nuclear Physics.

Beta Decay



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Some β emitters of interest

Nucleus	Energy	Half-life	Initial power
^{106}Ru	39.4 keV	1.02 yr	31.8 W/g
^{144}Ce	318 keV	285 days	25.5 W/g
^{60}Co	318 keV	5.3 yr	17.5 W/g
^{170}Tm	968 keV	129 days	11.9 W/g
^{90}Sr	548 keV	29.1 yr	0.92 W/g
^{86}Kr	687 keV	10.7 yr	0.59 W/g
^{137}Cs	514 keV	30.2 yr	0.43 W/g
^{147}Pm	224 keV	2.52 yr	0.34 W/g
^3H	18.6 keV	12.3 yr	0.33 W/g

Initial powers include daughter reactions: Kneels Atomic

Power Lab 2010, Nuclides and Isotopes: Chart of the Nuclides.

Statt & Wetskopf 1982, Theoretical Nuclear Physics, Segre 1977, Nuclear and Particle, DeHoff & Feshbach 1974, Theoretical Nuclear Physics.

β emitters with large decay energies ΔE have short half-lives unless decay requires a large emitted angular momentum L .

1. Are there any β emitters that are easier to produce and/or easier to use than those in the table?

2. Are there any ways to suppress the rate of β decay when it is not desired (e.g., to keep energy stored during a long interplanetary trip) and/or induce β decay when it is desired (e.g., when especially large amounts of output power are needed during an interplanetary mission)?

a. The β decay rate is controlled by the properties of the nucleus, which probably cannot be altered much without $\sim\text{MeV}$ of input energy, which would likely be prohibitively large. Nonetheless, it is good to consider all possibilities and conclusively rule them in or out.

b. Could nuclear angular momentum be altered enough to (temporarily) increase or decrease the β decay rate?

c. Could sufficiently strong electric, magnetic, electromagnetic, and/or other fields perturb nuclear states enough to (temporarily) increase/decrease the β decay rate?

d. Could the capture of a neutron, electron, antiproton, or other particle by the nucleus increase the β decay rate?

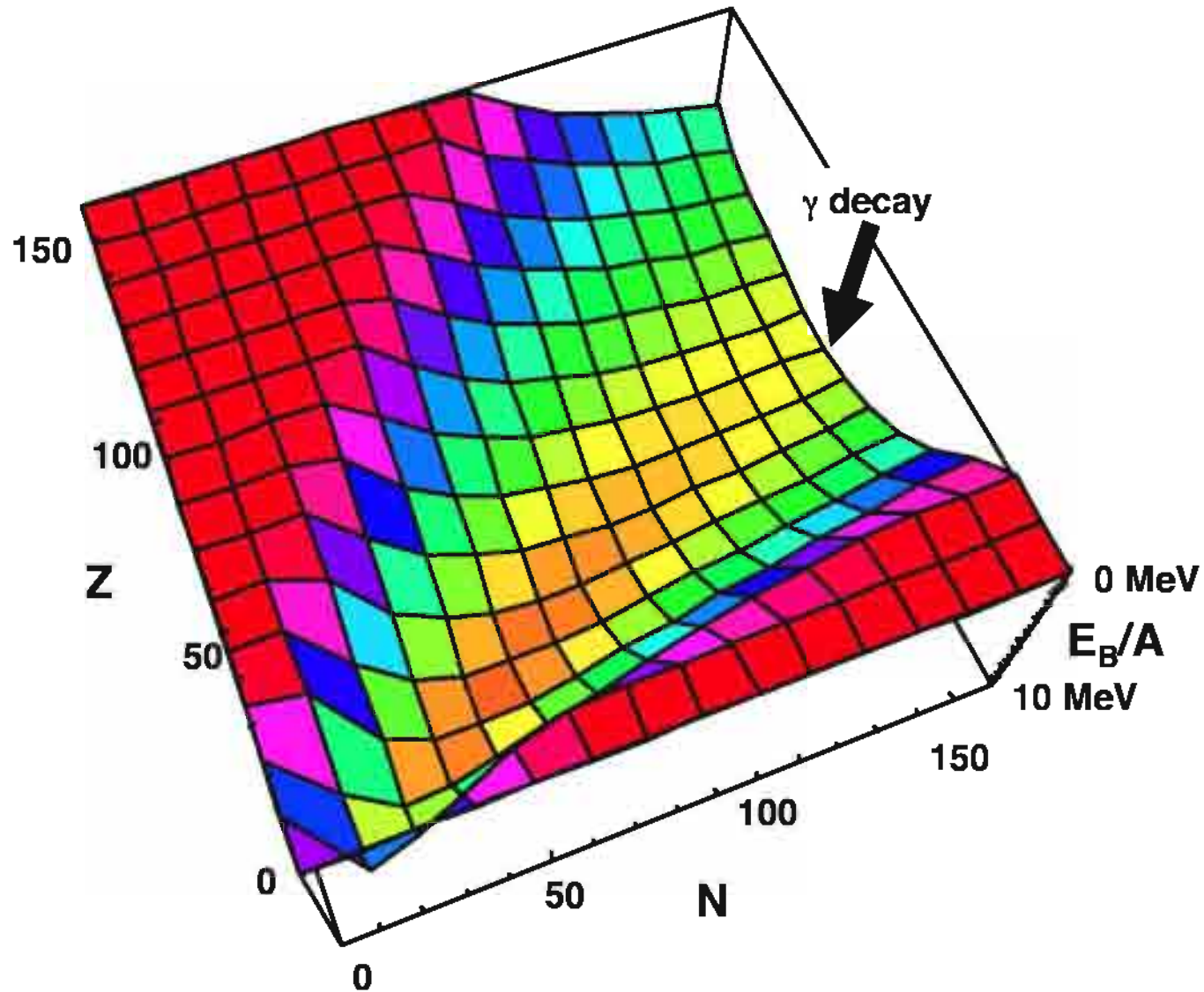
e. Could the β decay rate be increased by adding enough energy to the nucleus (via gamma rays, neutrons, or other means), then efficiently extracting that energy (plus the usual β decay energy) from the resulting β particle?

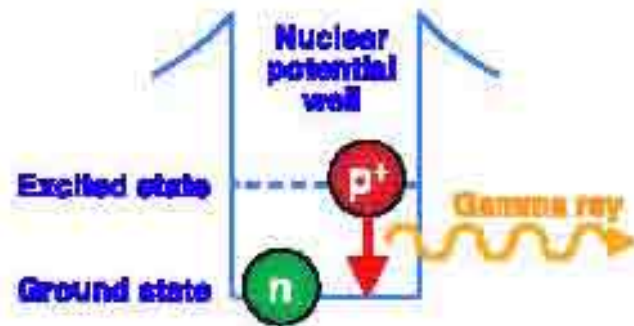
3. Are there better methods to convert the energy of the β particles to electricity?

a. The $\sim\text{mm}$ range of β particles in solids makes it quite difficult, but not necessarily impossible, to use anything other than some sort of thermal energy conversion process (usually with low conversion efficiencies).

b. See previous slide for some research directions that are applicable to β decay as well as α decay.

Binding Energy per Nucleon And Methods of Tapping It

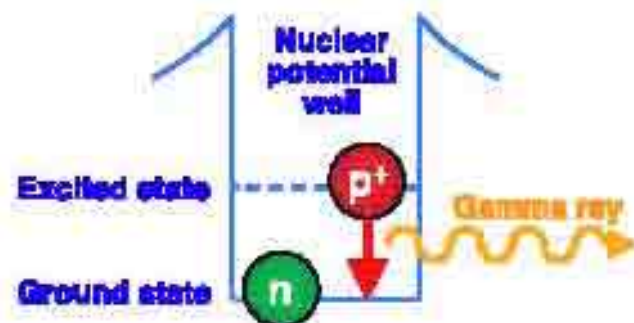




Gamma Decay

$$\tau_{1/2} \propto (10^6)^{\Delta J} (\Delta E)^{-(2\Delta J + 1)}$$

Isomers with large decay energies ΔE have very short half-lives unless the decay requires a large nuclear spin change ΔJ



Gamma Decay

$$\tau_{1/2} \propto (10^5)^{\Delta J} (\Delta E)^{-(2\Delta J + 1)}$$

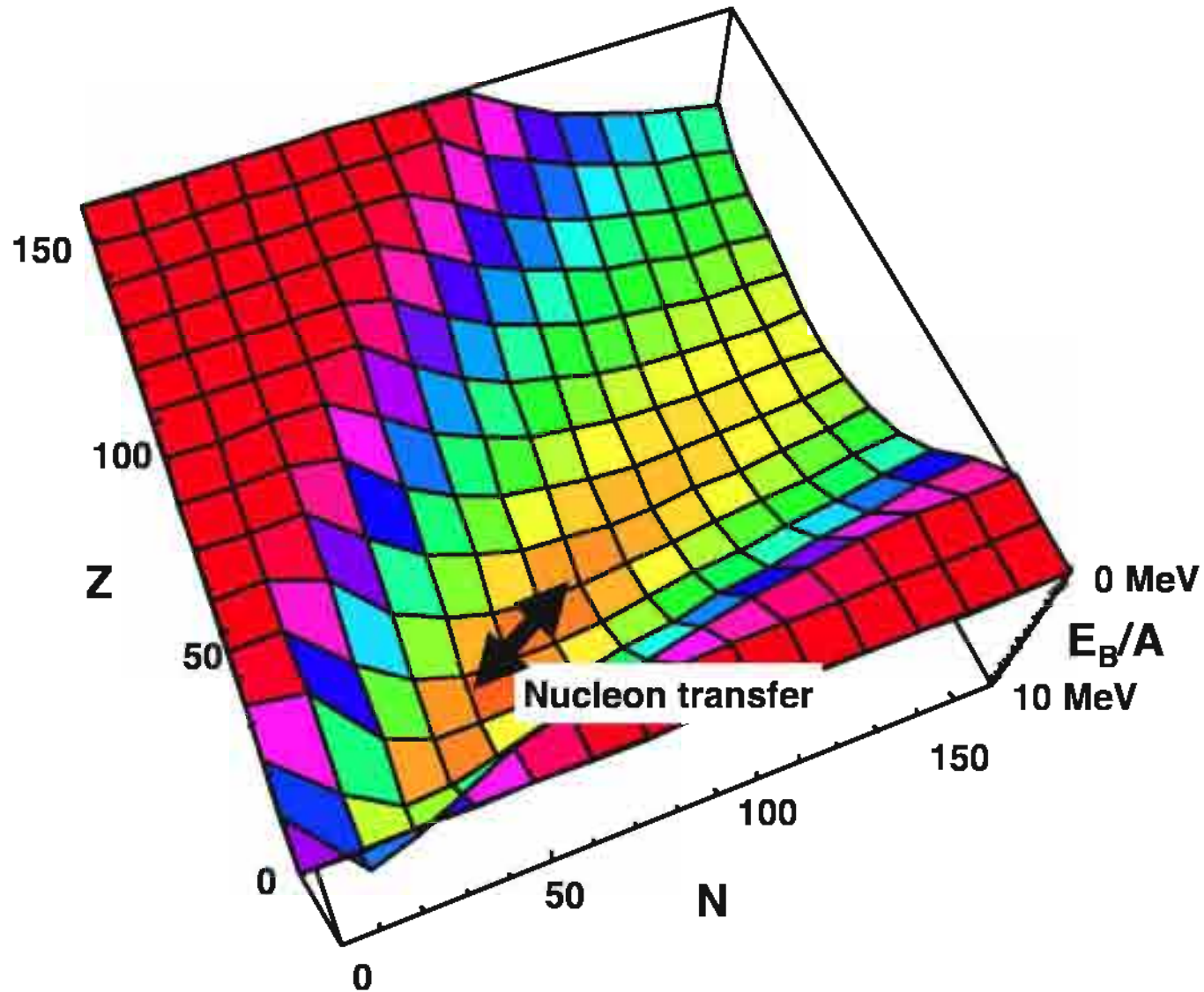
Isomers with large decay energies ΔE have very short half-lives unless the decay requires a large nuclear spin change ΔJ

Some Isomers of Interest

Nucleus	Energy	ΔJ	Half-life
¹⁷⁸ Hf	2.45 MeV	16	31 years
¹⁸⁰ Au	812 keV	10	2.3 days
¹⁸⁰ Ta	77.1 keV	8	>2x10 ¹⁶ yr
¹⁷⁷ Lu	970 keV	8	160.4 d
¹⁸² Ta	520 keV	7	15.8 min
¹⁰⁸ Ag	109 keV	5	418 yr
¹²⁶ Te	145 keV	5	57 days
²⁴¹ Am	48.6 keV	4	141 yr
⁹³ Nb	30.7 keV	4	16.1 yr
⁹² Tc	143 keV	4	6 hr
⁵⁸ Co	25.0 keV	3	9.0 hr
¹⁸⁰ Os	30.8 keV	3	5.8 hr
⁶⁰ Co	59 keV	3	10.5 min
¹⁸³ Ho	298 keV	3	1.1 sec

Baldwin et al 1991, Reviews of Modern Physics 63:387. Blatt & Weisskopf 1957, Reviews of Modern Physics 29:100. Boller et al 1999, Gamma-Ray Lasers. Becker 2008, AIP Proceedings 919:1-10. Belyaev 2007, www.sciencedirect.com/science/article/pii/S0370157107000000. Belyaev et al 2010, Nuclear Matter. Collins et al 1999, Physical Review C 59:034301. Collins et al 2001, Physical Review C 63:034301. Collins et al 2001, Hyperfine Interactions 139:1. Collins et al 2001, Laser Physics Letters 28:102. Gaponov & Hurn 2006, Physical Principles of Thermonuclear Explosions. Hahn 1921, Naturwissenschaften 9:164. Harouzi et al 2000, LLNL-TR-407891. Jain et al 2021, Nuclear Isomers: A Primer Kluwer 2007, www.kluweronline.com/ISBN/9781402020000/gamma-isomers.html. Lurie et al 1997, JASCH Report J97-97-110. Litz & Meriel 2004, www.sciencedirect.com/science/article/pii/S0370157104000000. Poirier et al 2007, Laser Physics 17:6:676. Poppe et al 1992, UCRL-JC-108028-Rev.1. Poirier 2007, Quantum Electronics 37:6:723. Bolvin et al 2004, Physics Today 57:5:21. Walker & Carroll 2007, Nuclear Physics News 17:2:11. Walker & Drobos 1998, Nature 393:58. Weisskopf 2008, Imaginary Weapons. Zaslavsky & Carroll 2002, Hyperfine Interactions 142:155. Zimmerman 2007, APB News 16:9:9.

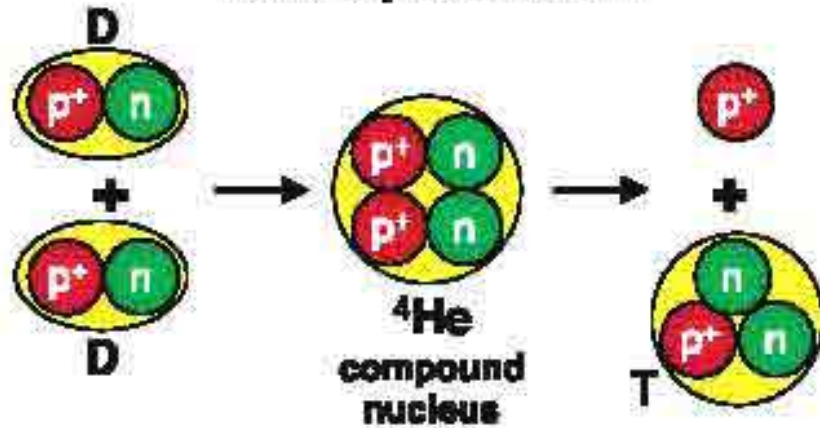
Binding Energy per Nucleon And Methods of Tapping It



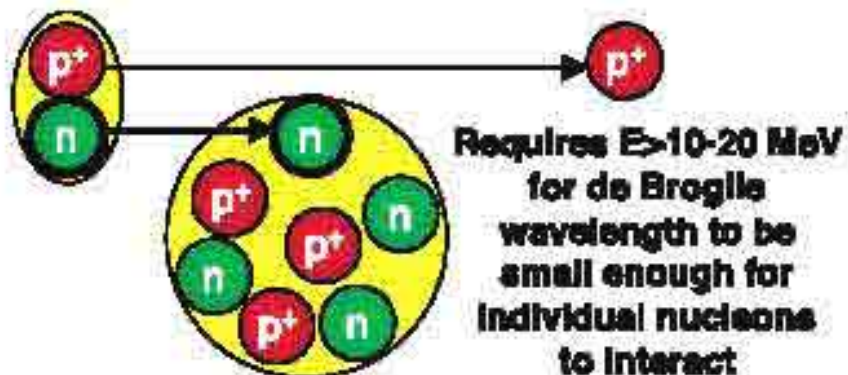
Nucleon Transfer Between Nuclei

Nuclei contact each other

**Temporarily form a compound nucleus
—that is just fusion:**



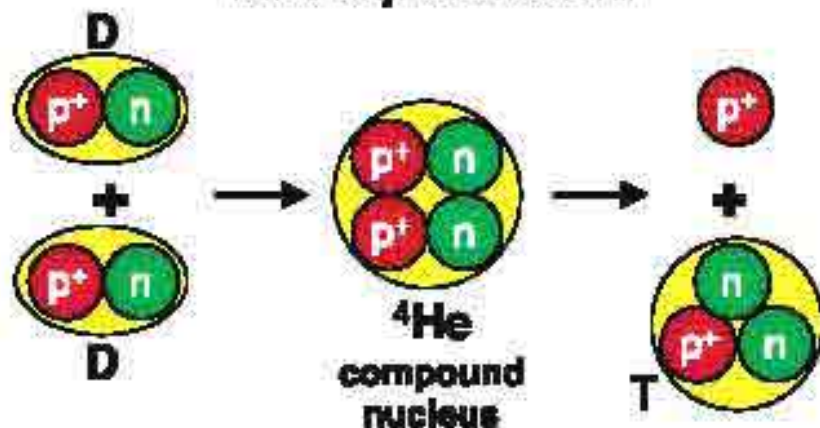
**Do not form a compound nucleus
—that is a direct reaction
(stripping or pickup):**



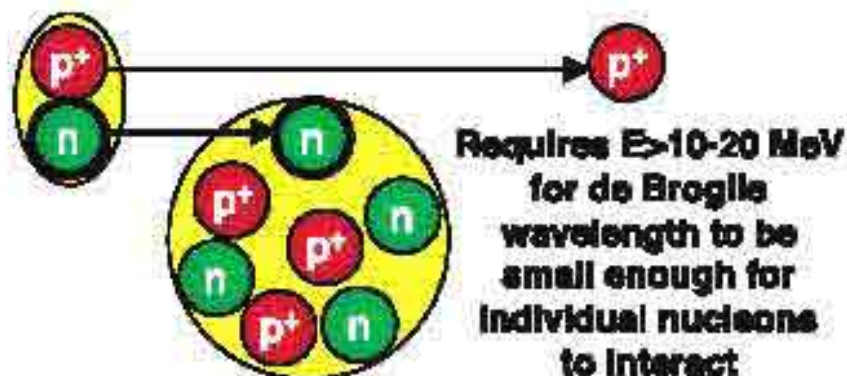
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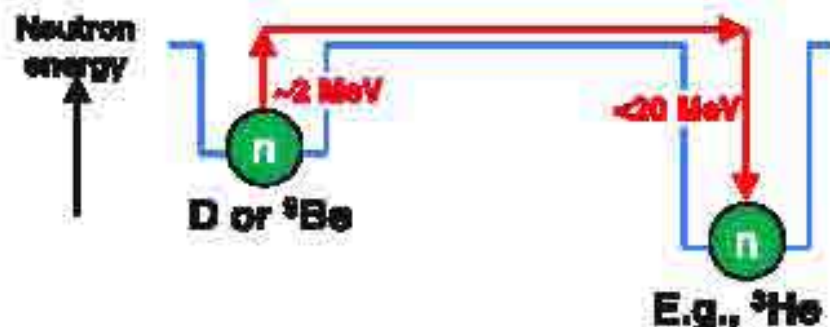
Temporarily form a compound nucleus
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Do not form a compound nucleus
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Nuclei not in contact



Much easier to transfer neutrons
than protons—no Coulomb barrier

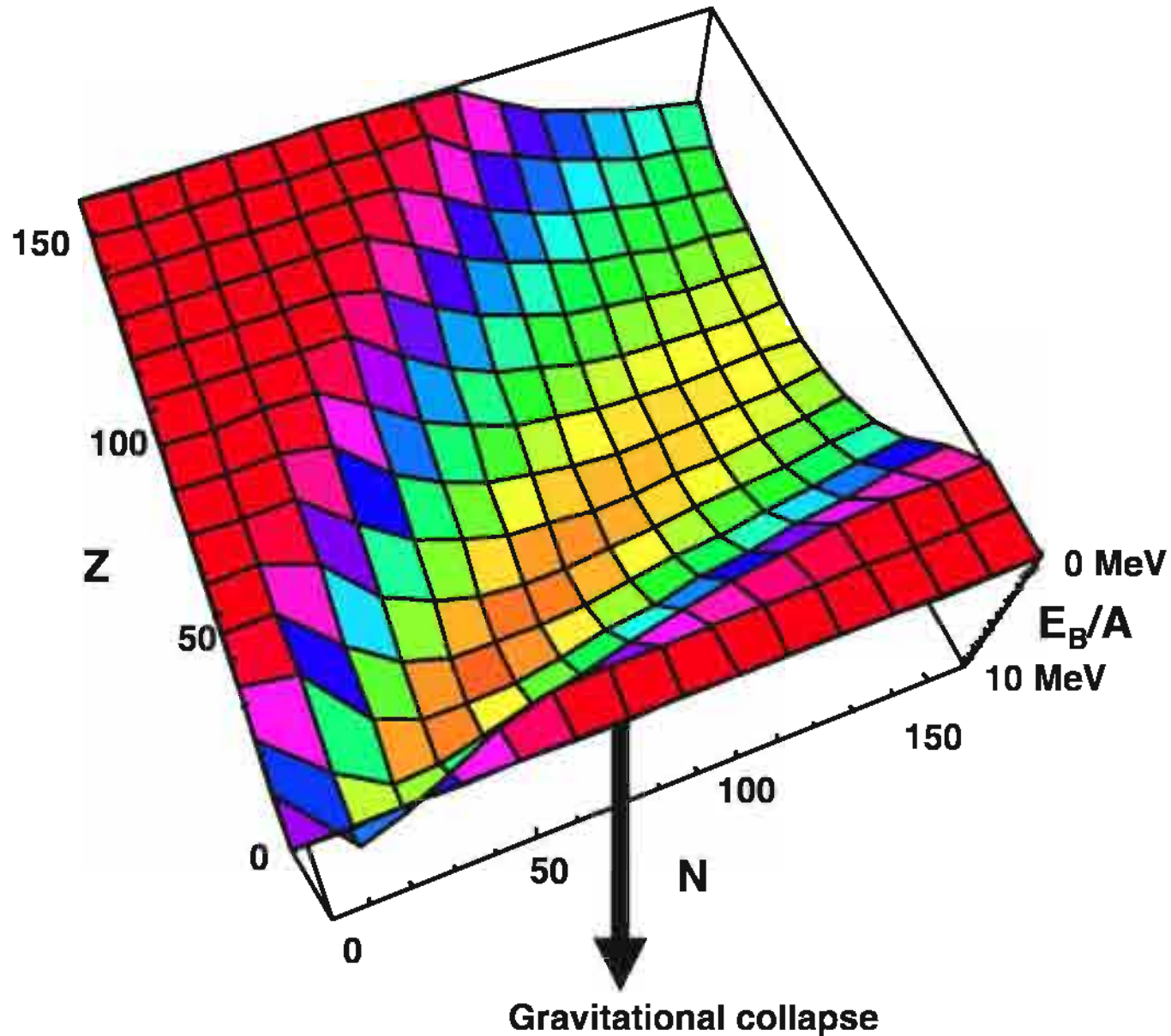
Difficult to supply input & remove
output energy without fission

Proposed magical neutron transfer
methods (no evidence so far):

- Meshuganon/meshugatron particle
- Polyneutrons
- Coherent neutron quantum states
- Lattice vibration energy in solids

Barricelli 2009, Defense Intelligence Agency Report DIA-08-0911-003. Berlinguette et al 2019, *Nature* 570:45. Hagelstein et al 2004, *New Physical Effects in Metal Deuterides*, www.kenr-cnr.org. Hagelstein & Chaudhary 2013, *Current Science* 105:4507. Hulzenga 1999, *Cold Fusion: The Scientific Placebo of the Century*. Landes & Hulzenga 1999, Report DOE/S-0073, www.ostlgon.gov/data/purl/5144772. Storms 2012, *A Student's Guide to Cold Fusion*, www.kenr-cnr.org.

Binding Energy per Nucleon And Methods of Tapping It



Gravitational Collapse

Extract energy from mass falling into black hole (Schwarzschild radius $R_s=2GM/c^2$)

Back-of-the-envelope Newtonian calculation of the total energy of a mass m in a circular orbit with radius r and velocity $v = (GM/r)^{1/2}$:

$$\begin{aligned} E &= mc^2 + 0.5mv^2 - (GMm/r) \\ &= mc^2 - (GMm)/(2r) \\ &= mc^2 [1 - (R_s)/(4r)] \end{aligned}$$

Convert up to $(R_s)/(4r)$ of infalling matter's rest mass to energy.

For closest stable orbit of nonrotating black hole, $r = 3R_s$:

Convert ~8% (actually 6% from more detailed calculations).

For closest stable orbit of maximally rotating black hole: $r = R_s/2$:

Convert ~50% (actually 42% from more detailed calculations).

For comparison, fusion converts <0.7% of rest mass to energy.

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Extract energy from the black hole itself

Nonrotating black hole:

- Hawking radiation (slow unless black hole is microscopic).

Rotating black hole—example processes:

- Penrose process for matter.
- Superradiant scattering for photons.
- Blandford-Znajek process for electromagnetic interactions.

DIY Black Hole

Implosion of Matter

Implode mass M to its
Schwarzschild radius R_s :

$$R = R_s = 2GM/c^2$$

Before matter becomes a black
hole, it becomes relativistic
neutrons with a huge positive
Fermi energy and a negligible
negative gravitational energy.

Total energy of $N = M/m_n$
neutrons compressed to R :

$$\begin{aligned} E_{\text{compr}} &= N E_{\text{avg Fermi}} \\ &= 0.6 (9\pi/4)^{1/3} (\hbar c N^{4/3}/R) \\ &= 0.6 (9\pi/4)^{1/3} (\hbar c/R) M^{4/3}/m_n^{4/3} \end{aligned}$$

Total energy of neutrons
compressed to R_s :

$$\begin{aligned} E_{\text{compr}} &= 0.3(9\pi/4)^{1/3}(\hbar c^3/G)M^{1/3}/m_n^{4/3} \\ &= 1.2 \times 10^{37} M_{\text{kg}}^{1/3} \text{ Joules} \\ &= 1.2 \times 10^{35} \text{ Joules for 1 mg target} \end{aligned}$$

Required energy is actually much
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Focused Energy

Compress a mass M within its Schwarzschild radius R_s :

$$M = (R_s c^2)/(2G)$$

OR

Compress an equivalent amount of energy within R_s :

$$\begin{aligned} E &= Mc^2 = (R_s c^4)/(2G) \\ &= 6.07 \times 10^{43} R_{s, \text{ meters}} \text{ Joules} \end{aligned}$$

Diffraction limits focused size of electromagnetic waves. Best to use X- or γ -rays.

Focusing X-rays to create a black hole of atomic size ($\sim 10^{-10}$ meters) would require $\sim 10^{33}$ Joules of X-ray energy.

(NIF is only 4×10^6 Joules IR.)

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Particle Collider

Energy to create a black hole:

$$\begin{aligned} E &= Mc^2 = (R_s c^4)/(2G) \\ &= 3.79 \times 10^{62} R_{s, \text{ meters}} \text{ eV} \end{aligned}$$

Planck length—smallest size:

$$\begin{aligned} L_p &= (\hbar G/c^3)^{1/2} \\ &= 1.62 \times 10^{-35} \text{ meters} \end{aligned}$$

$R_s \sim L_p$ for smallest black hole:

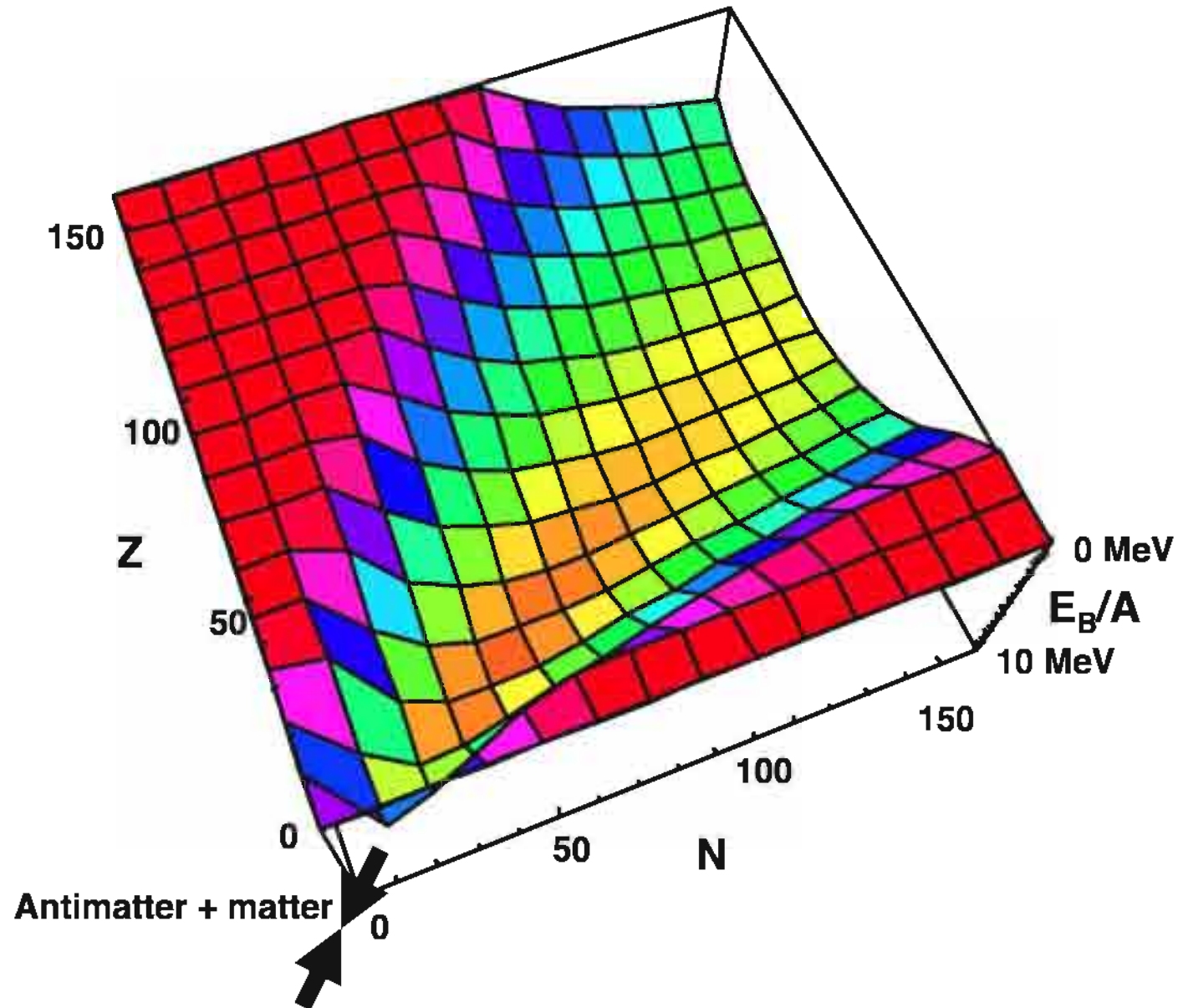
$$E \sim 6 \times 10^{27} \text{ eV}$$

(Large Hadron Collider $\sim 10^{13}$ eV.)

Any help from new physics effects? (No signs so far.)

Tiny black holes would quickly evaporate via Hawking radiation.

Binding Energy per Nucleon And Methods of Tapping It



Antimatter

Use

Antimatter + matter annihilation

- 100% of mass is converted to energy
(vs. $<0.7\%$ for fusion, $\sim 0.1\%$ for fission)

No natural sources of antimatter

- Useful for energy storage
but not energy production

Interstellar rocket propulsion is most important application

- Needs highest possible energy density
- Limits casualties if confinement fails

Brillouin limit on nonneutral storage:

- Rest energy density of antiparticles
 $<$ energy density of confining field
- Little better than just storing energy in
the form of the electric/magnetic field
- Must keep antimatter (nearly) neutral as
antiprotons + positrons (anti-hydrogen)

Energy produced as pions & γ rays

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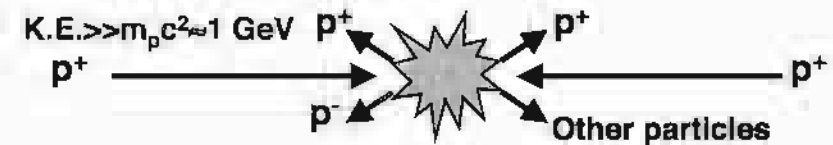
- Rest energy density of antiparticles < energy density of confining field
- Little better than just storing energy in the form of the electric/magnetic field
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Energy produced as pions & γ rays

Production

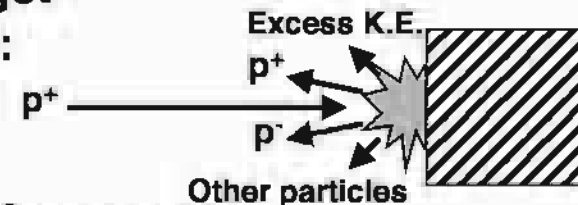
Much more difficult to make antiprotons (p^-) than positrons (e^+)

Proton (p^+) beam-beam collider:



- < 2×10^{-3} of K.E. converted into p^-
- < 10^{-5} g of p^- per year
- Colliding other particles even worse

Beam-target collider:



- > 100 g of p^- per year
- < 2×10^{-4} of K.E. converted into p^-

Converting EM field into $p^- + p^+$:

- Requires unattainable field strengths
- Still creates lots of unwanted particles

Binding Energy per Nucleon And Methods of Tapping It

